

Multi-sensor Data Fusion For Lane Boundaries Detection Applied To Autonomous Vehicle

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PhD candidate – 14th January 2022

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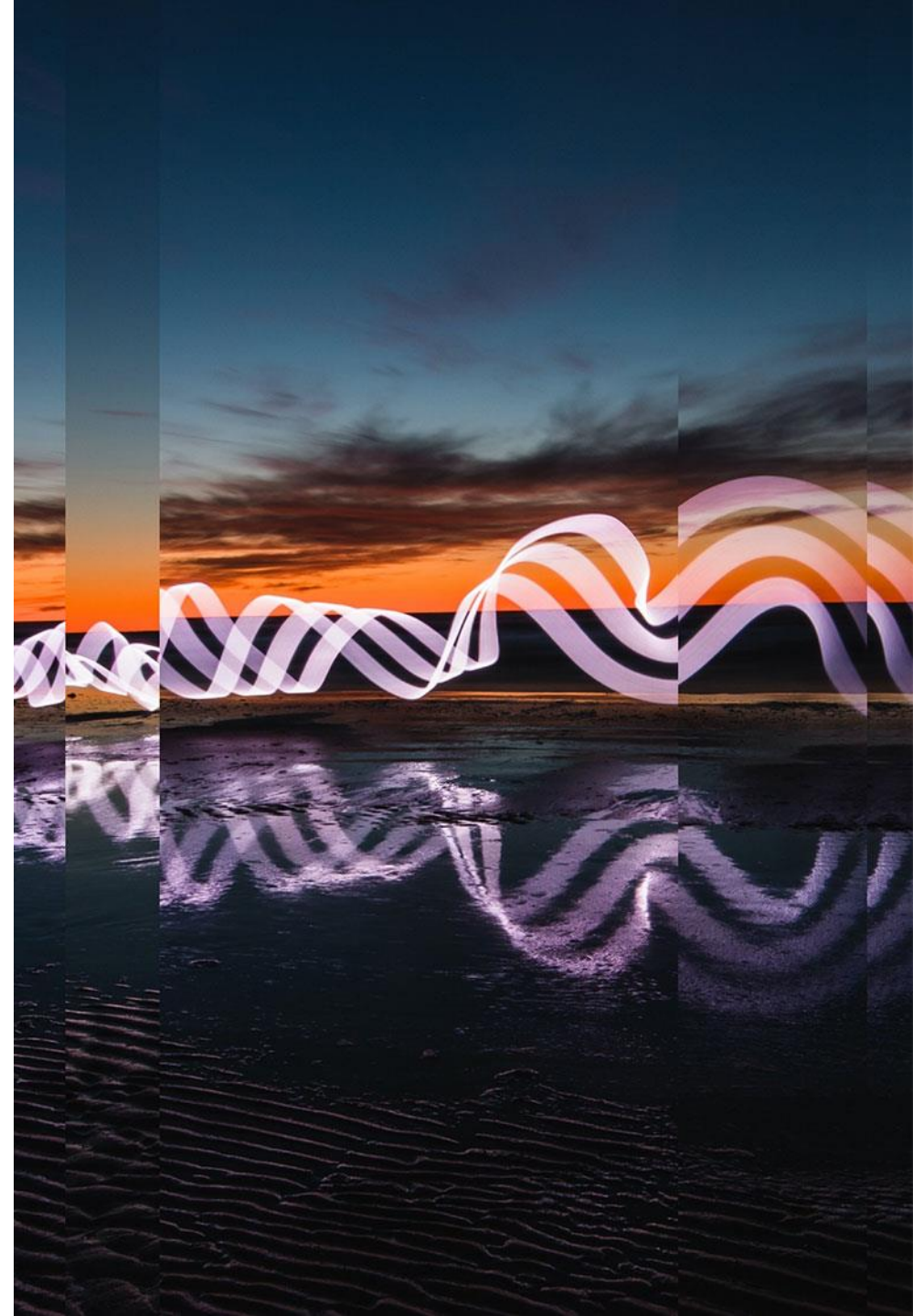
**Renault
Group**



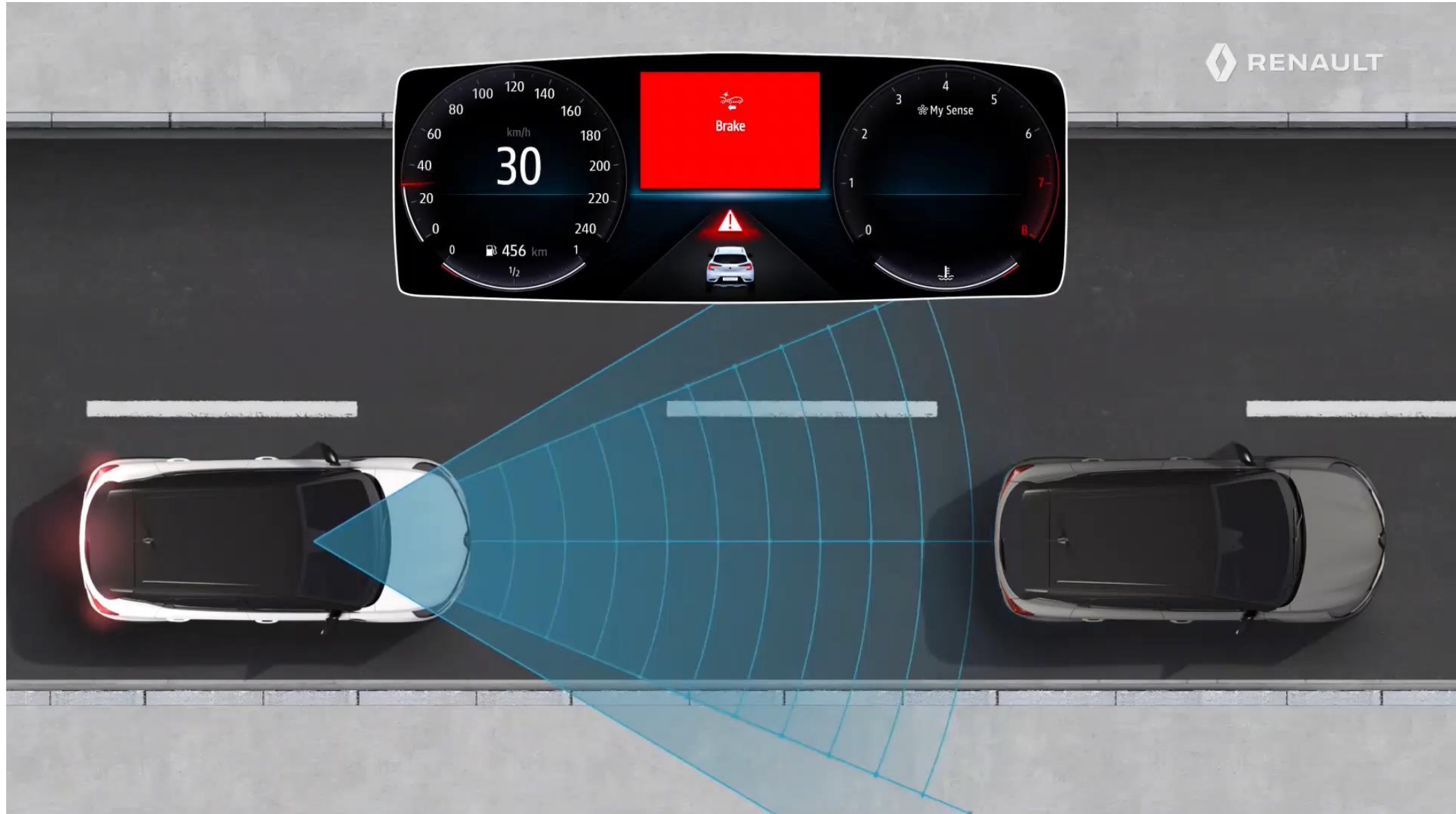
- 01** Thesis introduction
- 02** Problem formulation
- 03** Multi-sensor fusion for lane boundaries estimation
- 04** Map-aided multi-sensor fusion for lane boundaries estimation
- 05** Conclusions

01

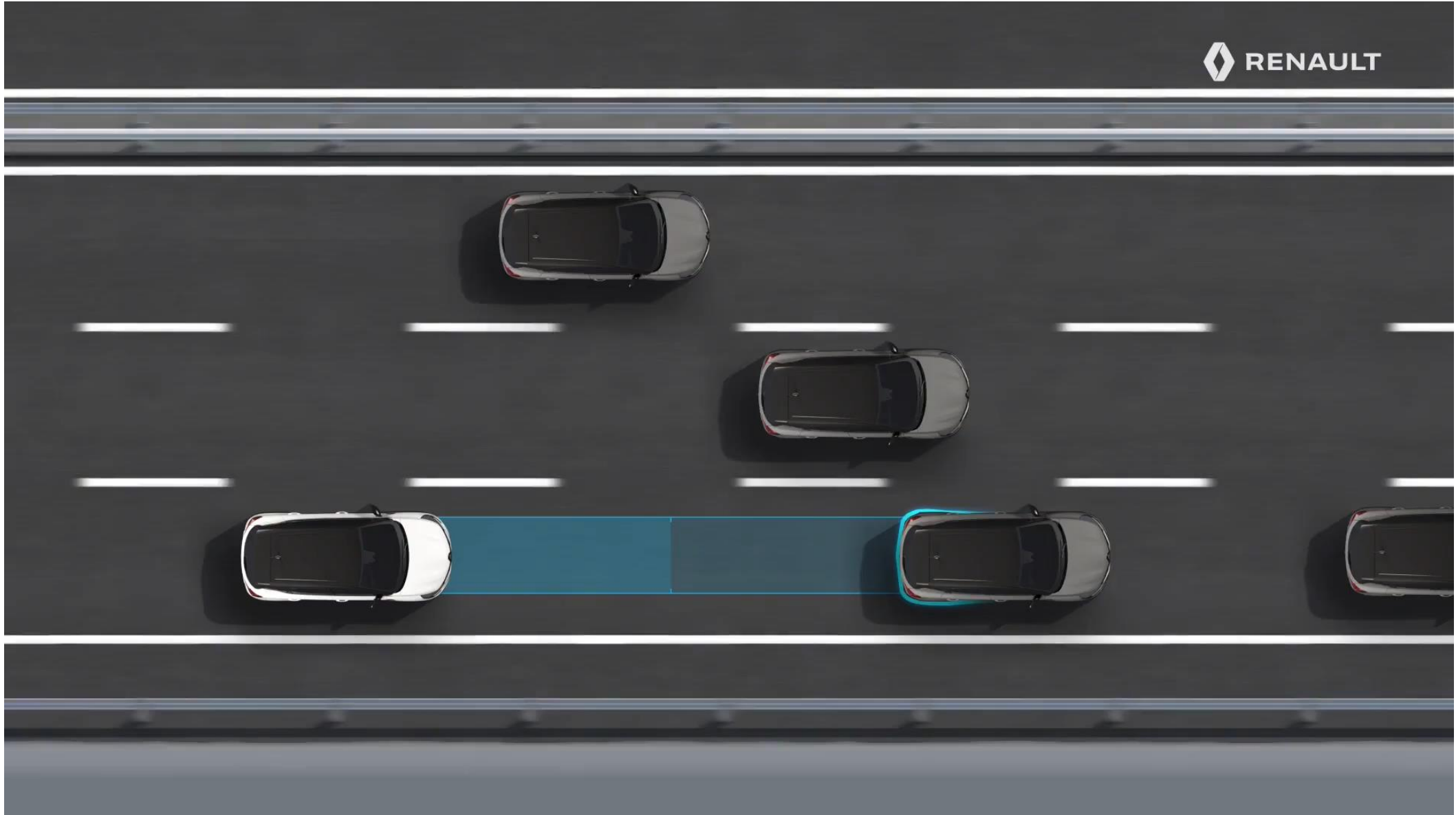
Thesis introduction



01 INTRODUCTION AD & ADAS



01 INTRODUCTION AD & ADAS



01 INTRODUCTION AD & ADAS



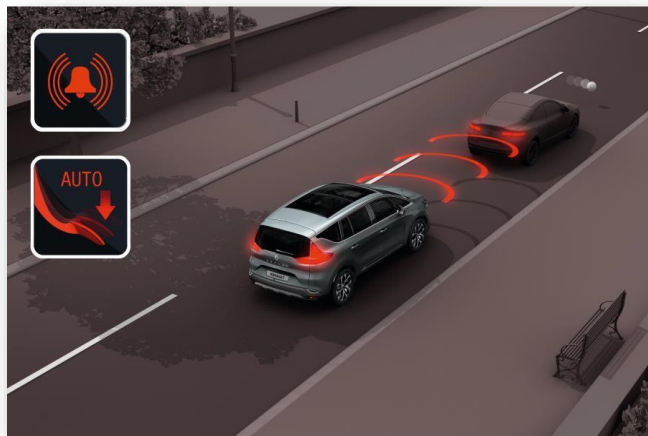
Informative ADAS

- Lane Departure Warning (LDW)
- Blind Spot Warning (BSW)
- Parking Sensor
- Driver Monitoring System (DMS)



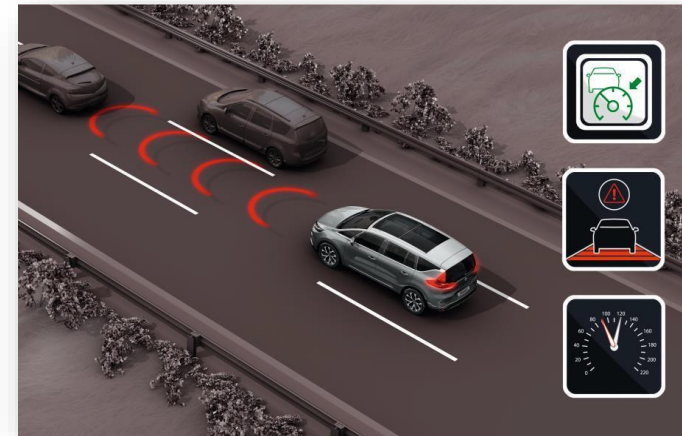
Actuating ADAS

- Adaptive Cruise Control (ACC)
- Lane Keeping Assistance (LKA)
- Lane Centering Assistance (LCA)
- Automatic Emergency Braking (AEB)
- Traffic Jam Pilot (TJP)
- Automatic Parking

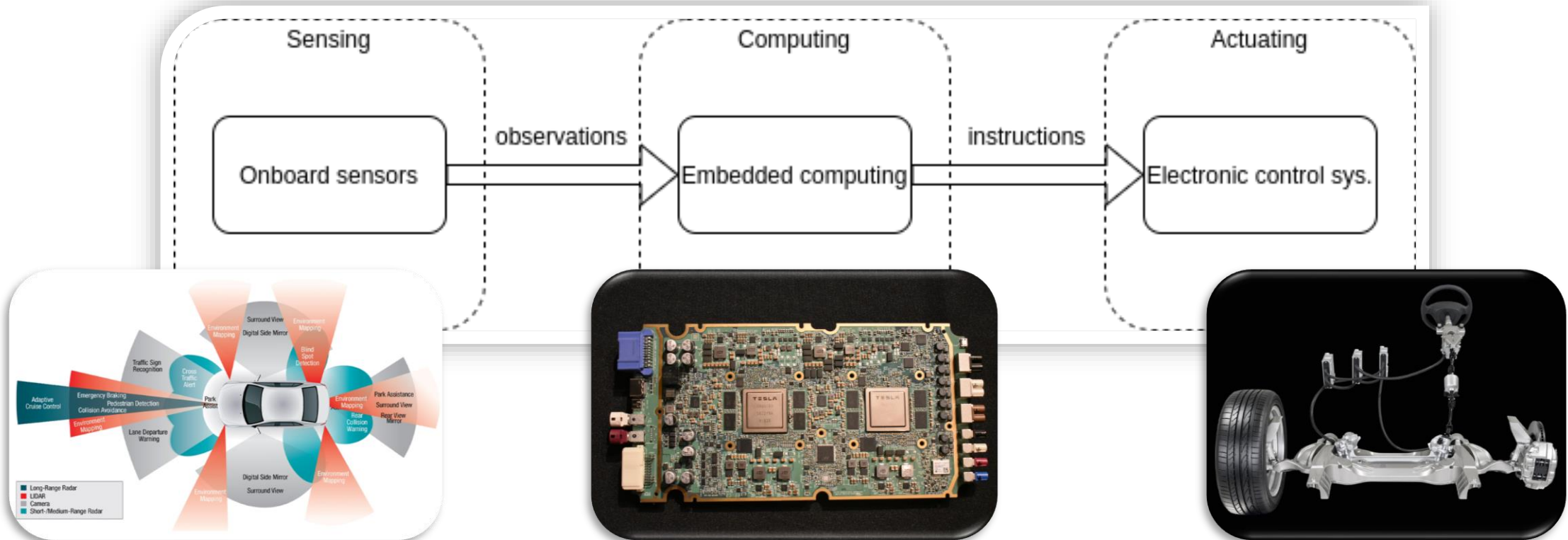


Automated driving

- Level 0 – No Automation
- Level 1 – Driver Assistance
- Level 2 – Partially Automated Driving
- Level 3 – Conditionally Automated Driving
- Level 4 – Highly Automated Driving
- Level 5 – Fully Automated Driving



1. Sensing – On board sensors
2. Computing – Embedded computing
3. Actuating – Electronic control systems



THESIS SCOPE : MULTI-SENSOR FUSION

- Perception diversity compensates sensor weaknesses

SENSOR TECHNOLOGIES : PROS & CONS								
		 Dazzling light	 Harsh weather	 Guardrails	 Lines	 Black objects	 Low contrast	 Occlusion
RADAR 								
LIDAR 								
CAMERA 								

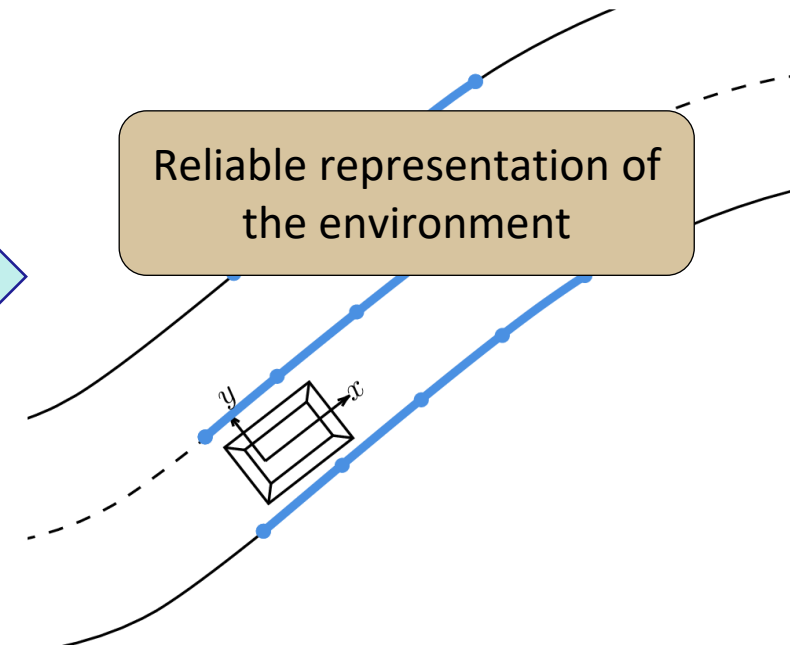
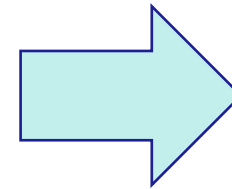
THESIS SCOPE : INDUSTRIAL CONTEXT (1)

- Car manufacturers integrate sensing solutions from Tier-1 suppliers : **smart sensors**

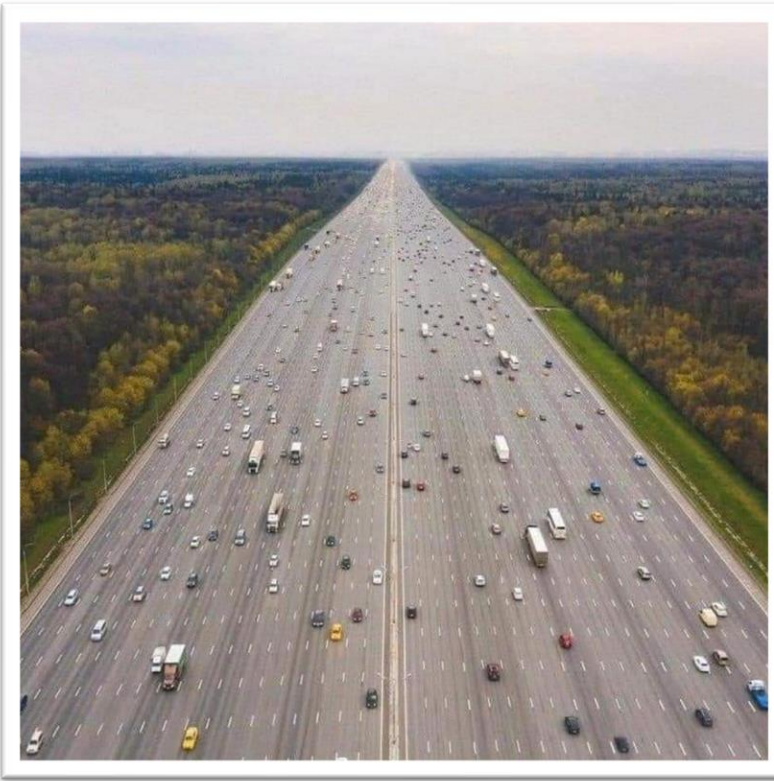


THESIS SCOPE : INDUSTRIAL CONTEXT (2)

- This work is developed within:
 - Sivalab (Hediasyc X Renault joint laboratory)
 - Renault's Fusion Team (DEA-LEA1: Algorithmes Fusion et Véhicule Autonome)
- ADAS software development platform available
- Ad-hoc equipped Renault Espace for Conditionally Automated Driving L3 (Level 3)



- Oriented lane corridors enable safe and predictable navigation for road users



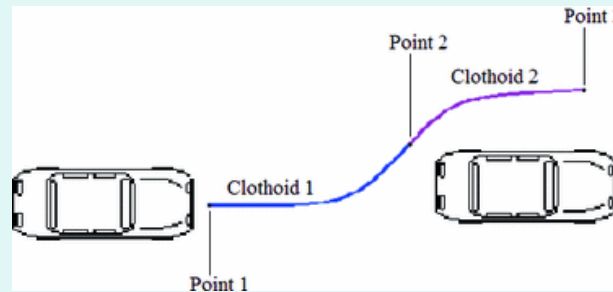
- Because of geographical constraints, roads are designed connecting straight and circular segments with *clothoid segments*

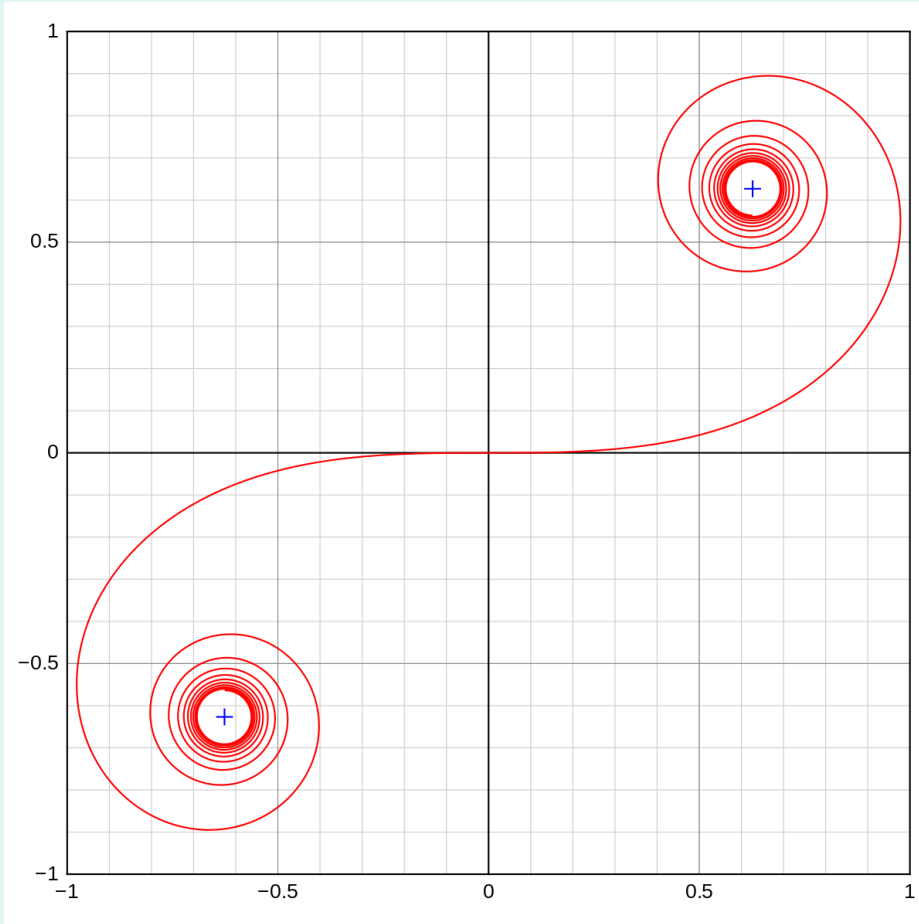
- A *Clothoid* is a curve whose curvature changes linearly with its curve length
- Its Cartesian coordinates are given by the Fresnel integrals :

$$x(s) = x_0 + \int_0^s \cos \left(\frac{1}{2} \kappa_1 \tau^2 + \kappa_0 \tau + \psi_0 \right) d\tau, s \in [0, l]$$

$$y(s) = y_0 + \int_0^s \sin \left(\frac{1}{2} \kappa_1 \tau^2 + \kappa_0 \tau + \psi_0 \right) d\tau, s \in [0, l]$$

- Application of clothoids to road designed allow comfortable transitions road segments:





$$x(s) = x_0 + \int_0^s \cos \left(\frac{1}{2} \kappa_1 \tau^2 + \kappa_0 \tau + \psi_0 \right) d\tau, s \in [0, l]$$

$$y(s) = y_0 + \int_0^s \sin \left(\frac{1}{2} \kappa_1 \tau^2 + \kappa_0 \tau + \psi_0 \right) d\tau, s \in [0, l]$$

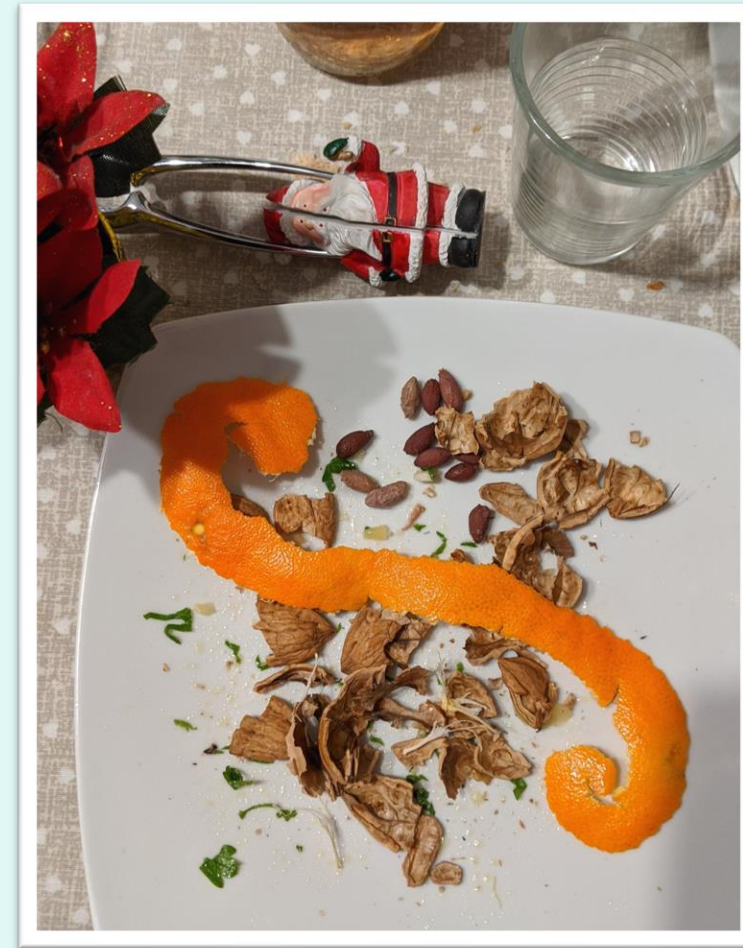
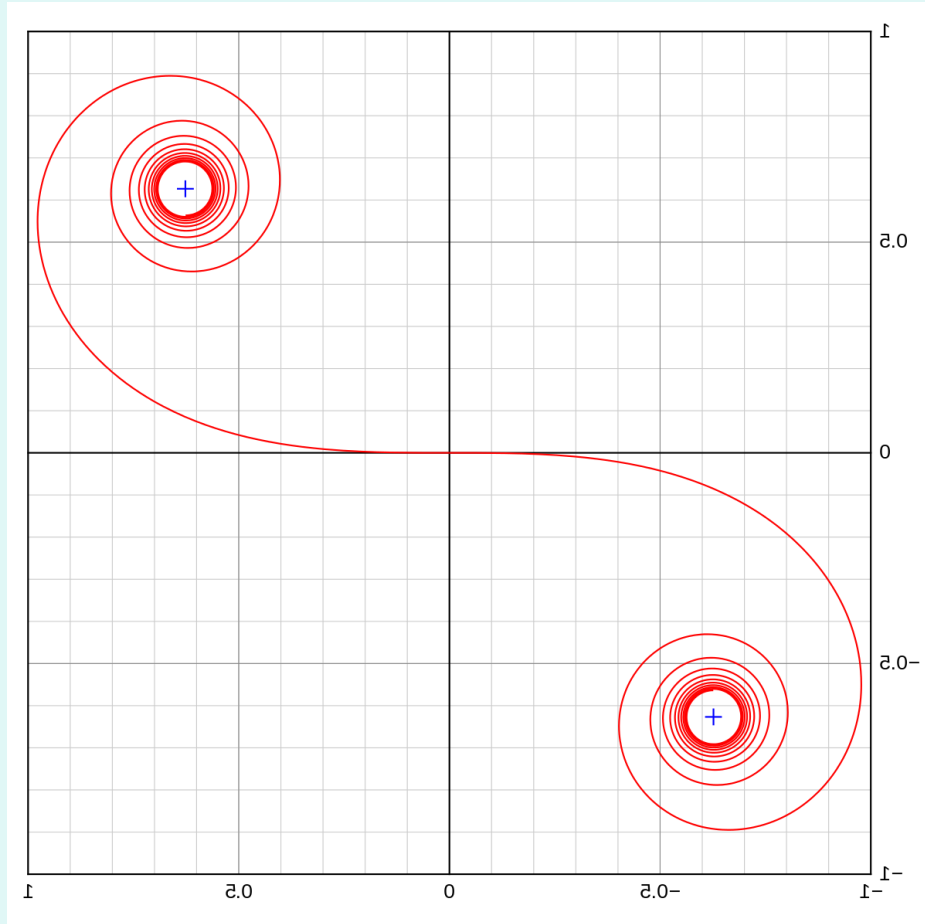
x_0 starting point abscissa

y_0 starting point ordinate

ψ_0 starting orientation angle

κ_0 starting curvature

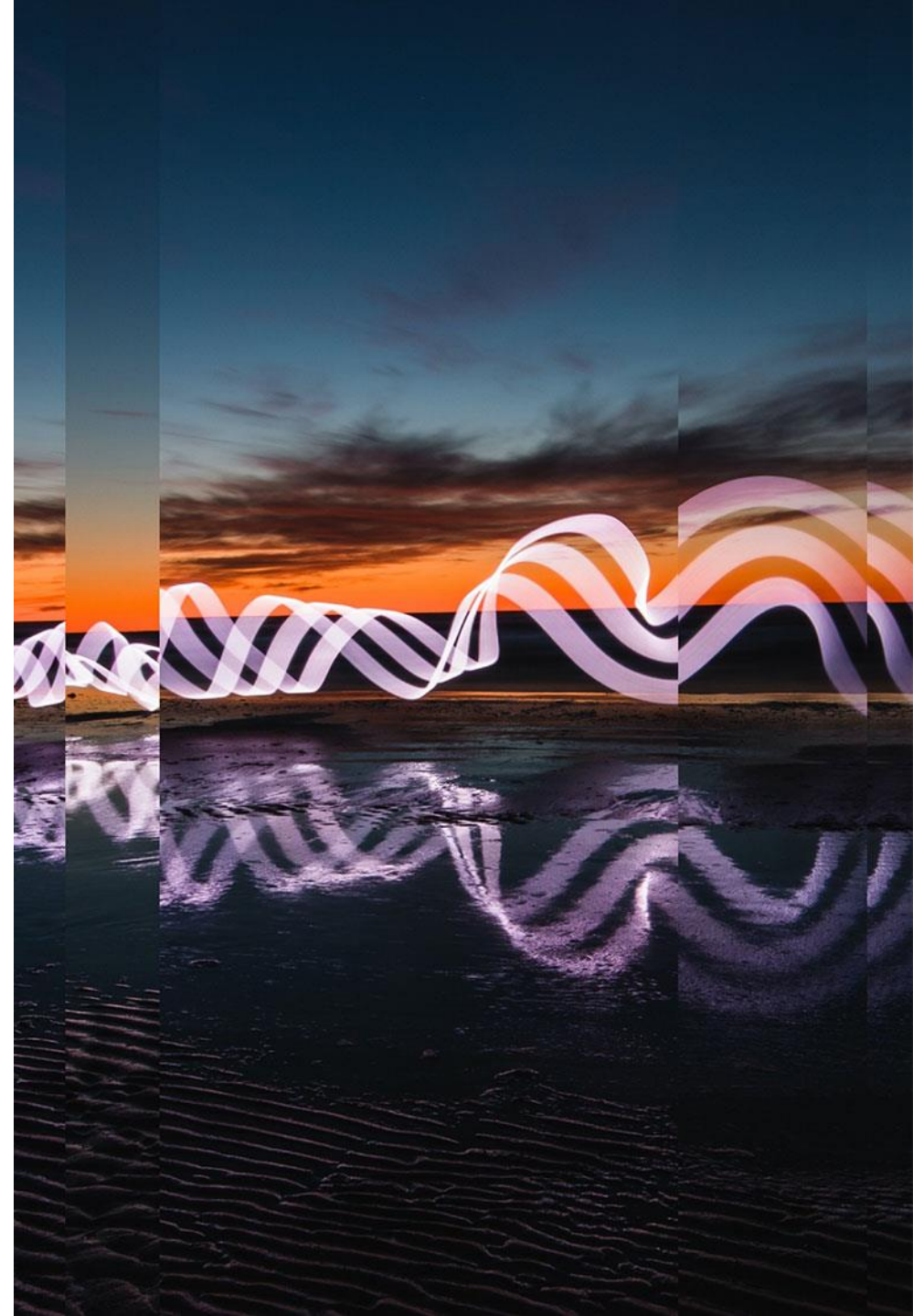
κ_1 curvature rate



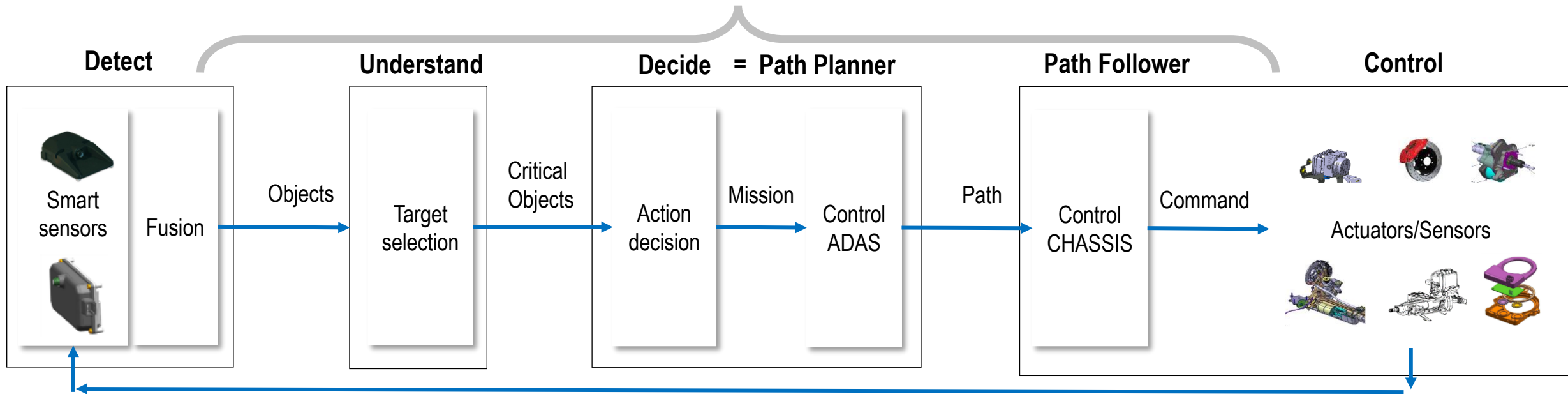
Bartholdi, Laurent & Henriques, André. (2012). Orange Peels and Fresnel Integrals. *The Mathematical Intelligencer*. 34. 10.1007/s00283-012-9304-1.

02

Problem formulation



AUTOMATED DRIVING PIPELINE : ADOPTED PIPELINE

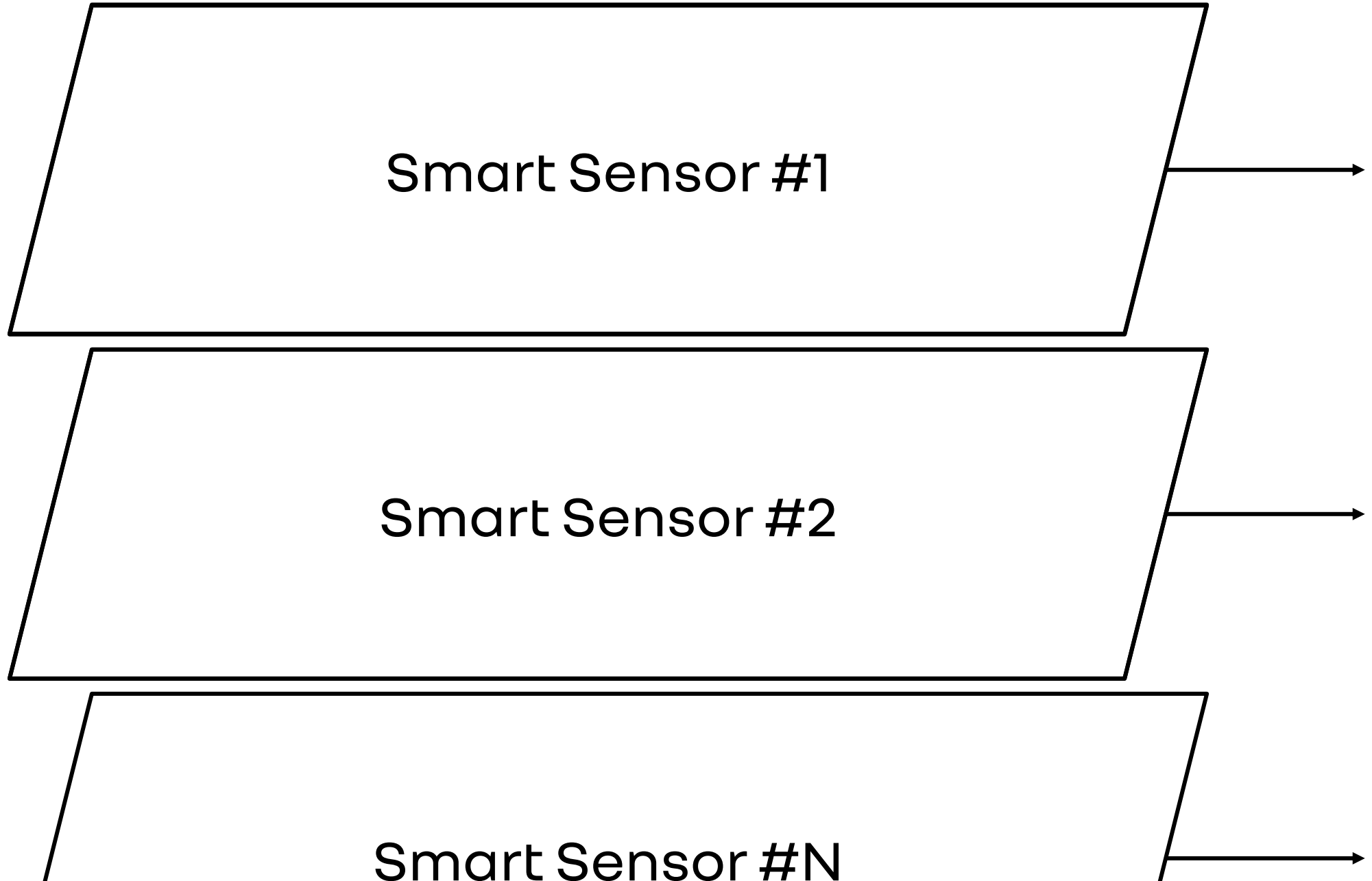


ADAS & AD
Algo Fusion

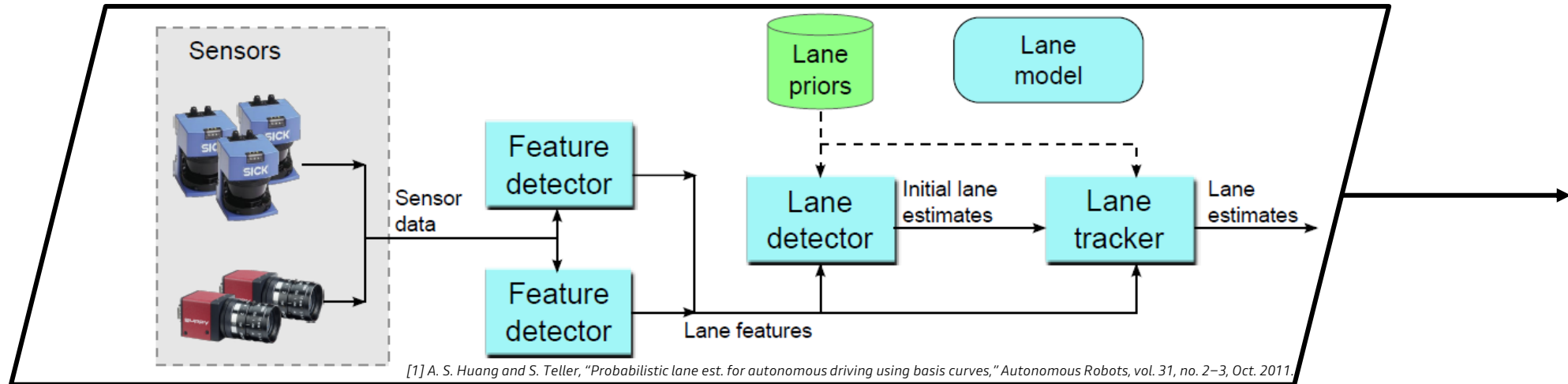
ADAS & AD
Control laws

CHASSIS
Control laws

SMART SENSORS : STATE OF THE ART

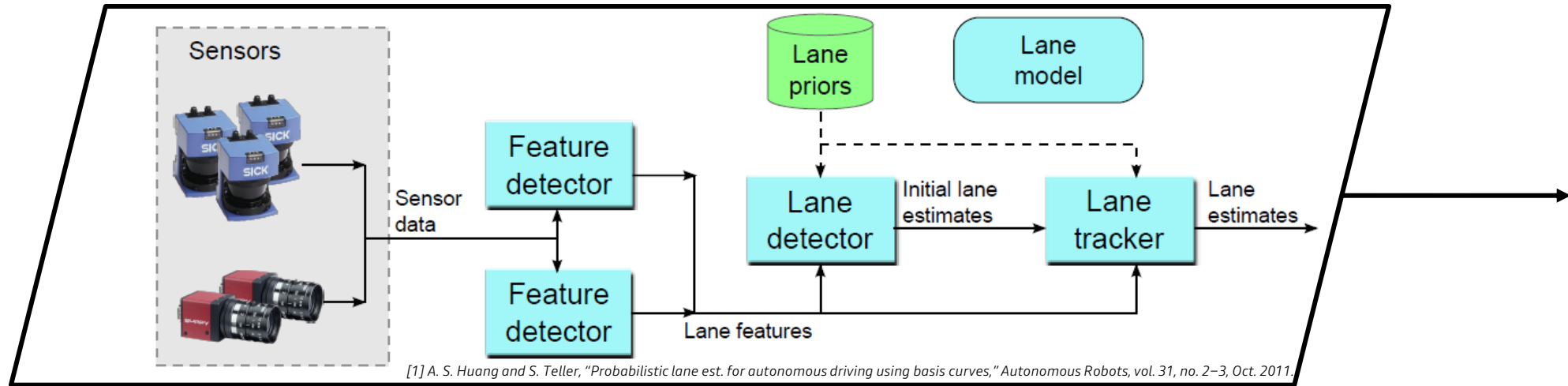


SMART SENSORS : STATE OF THE ART

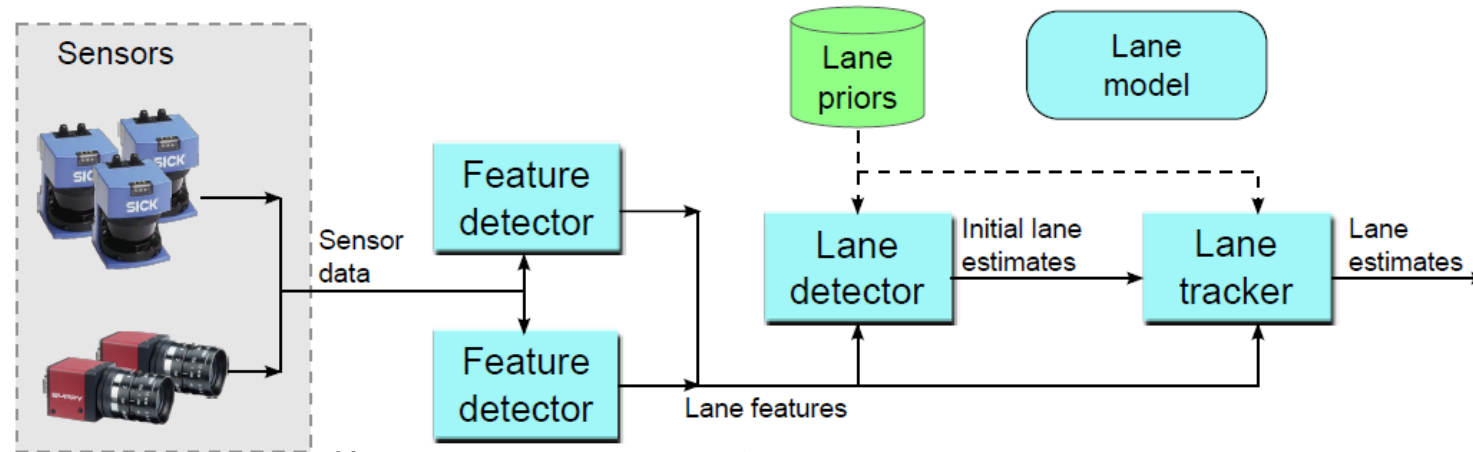


Smart Sensor #2

Smart Sensor #N

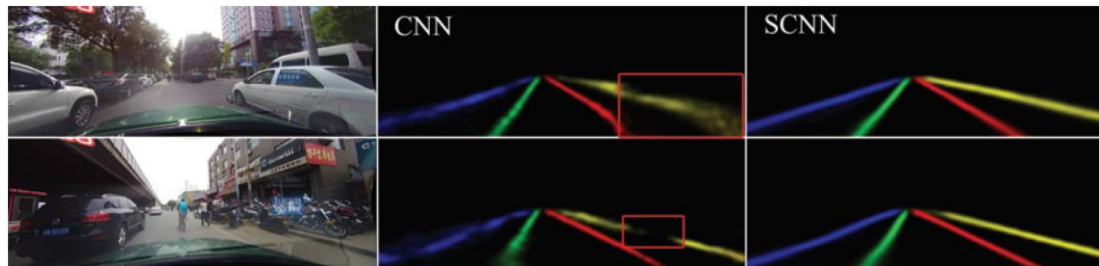


1. Feature extraction
2. Detection and tracking
3. Lane (boundary) model

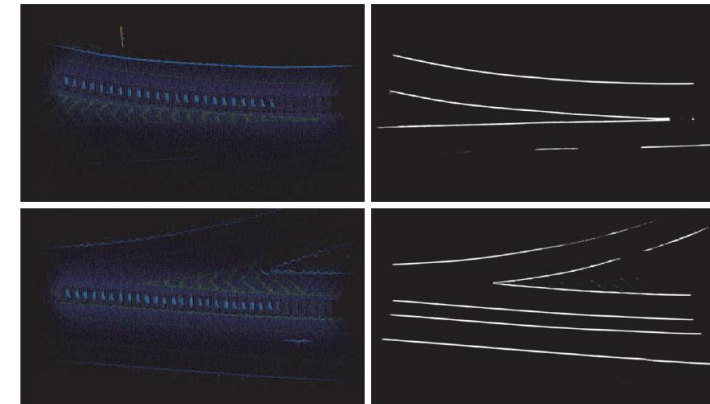


[1] A. S. Huang and S. Teller, "Probabilistic lane est. for autonomous driving using basis curves," *Autonomous Robots*, vol. 31, no. 2-3, Oct. 2011.

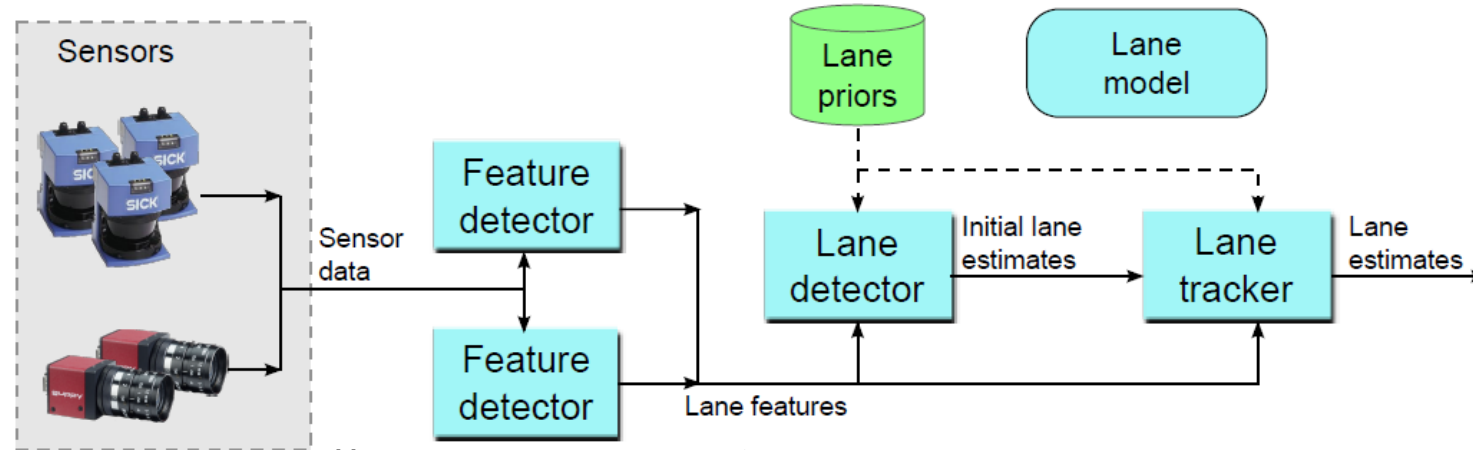
1. Feature extraction
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3. Lane (boundary) model



[2] X. Pan, J. Shi, P. Luo, X. Wang, and X. Tang, "Spatial as Deep: Spatial CNN for Traffic Scene Understanding"

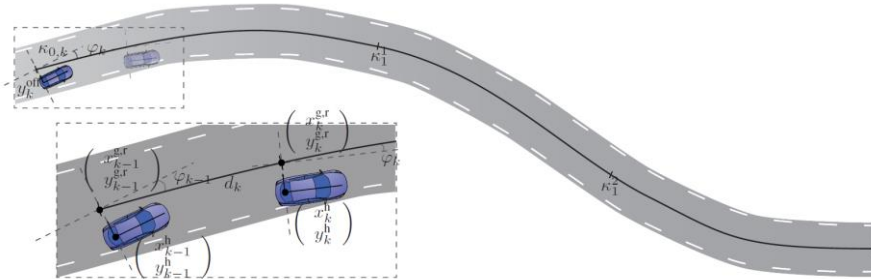


[3] B. He, R. Ai, Y. Yan, and X. Lang, "Lane marking detection based on Convolution Neural Network from point clouds," in *2016 IEEE 19th International Conference on Intelligent Transportation Systems (ITSC)*, 2016, pp. 2475-2480

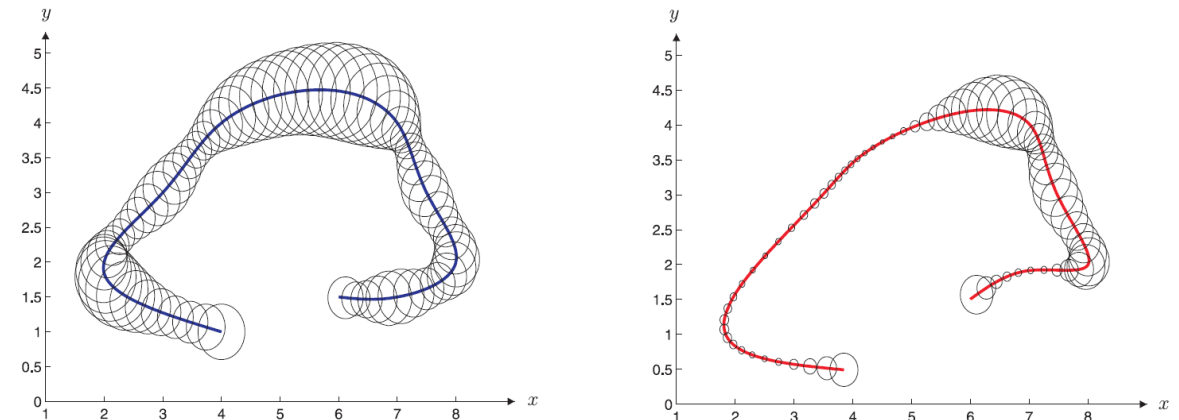


[1] A. S. Huang and S. Teller, "Probabilistic lane est. for autonomous driving using basis curves," *Autonomous Robots*, vol. 31, no. 2-3, Oct. 2011.

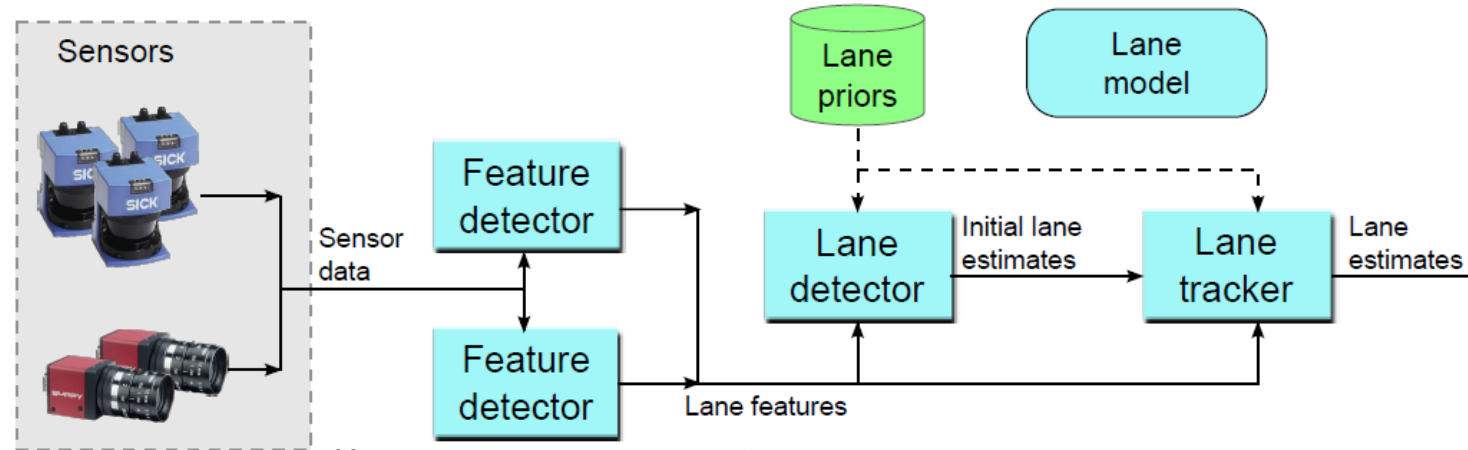
1. Feature extraction
2. Detection and tracking
3. Lane (boundary) model



[4] M. Fatemi, L. Hammarstrand, L. Svensson, and A. F. Garcia-Fernandez, "Road geometry estimation using a precise clothoid road model and observations of moving vehicles," 2014, pp. 238-24



[5] C. Hasberg and S. Hensel, "Online-Estimation of Road Map Elements using Spline Curves,"

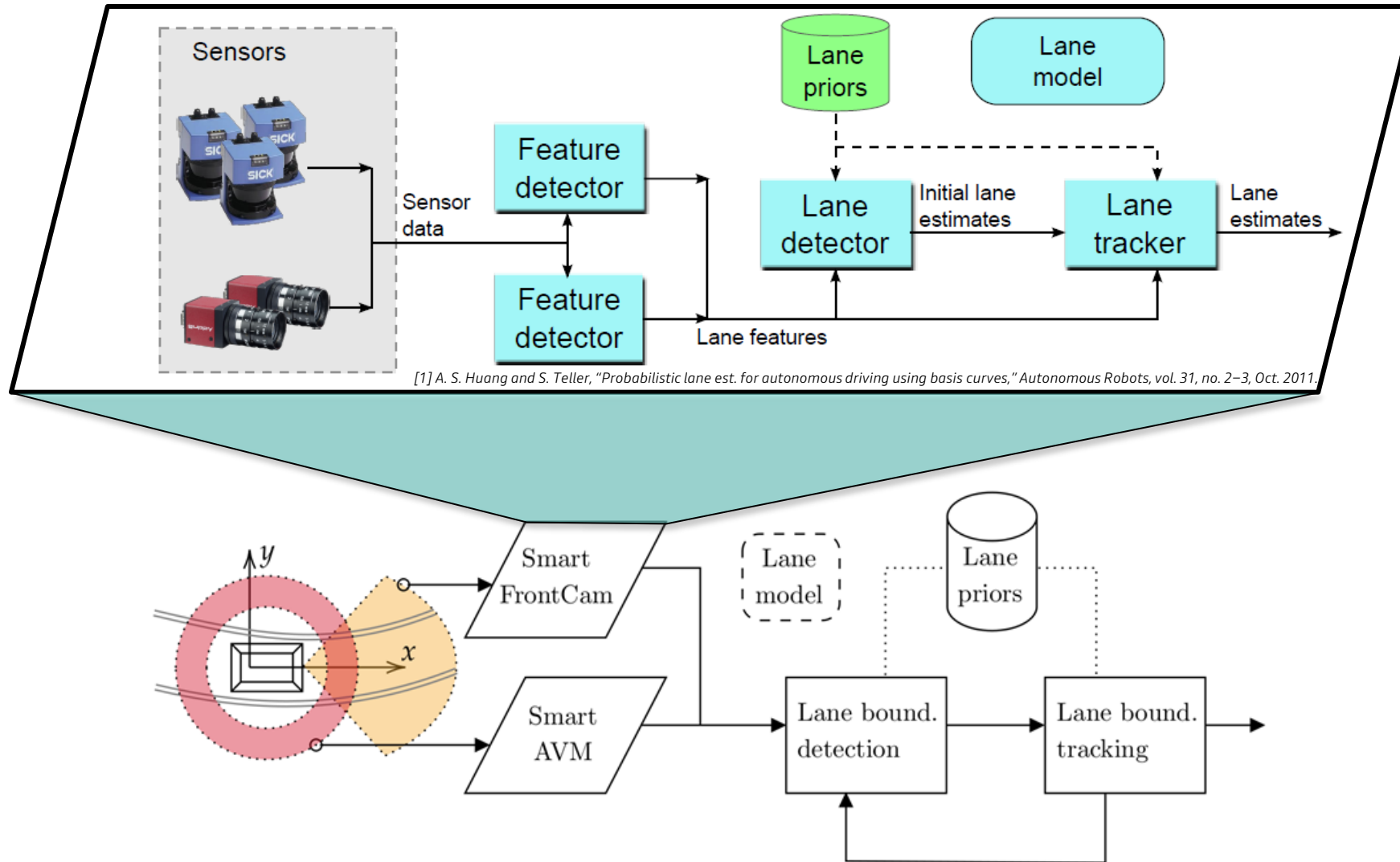


[1] A. S. Huang and S. Teller, "Probabilistic lane est. for autonomous driving using basis curves," *Autonomous Robots*, vol. 31, no. 2-3, Oct. 2011.

1. Feature extraction
2. Detection and tracking
3. Lane (boundary) model
 - Parametric: straight line, polynomials
 - Non-parametric: pixels
 - Semi-parametric: spline

02 PROBLEM FORMULATION

THESIS USE CASE



- Two smart sensors: Smart FrontCam and Smart AVM

SMART SENSOR MODEL

- Smart sensor delivery contains lane boundaries detection
- Single measurements describe the form of the lane boundary
- In the L3 sensor set, both Smart Camera and Smart AVM deliver:

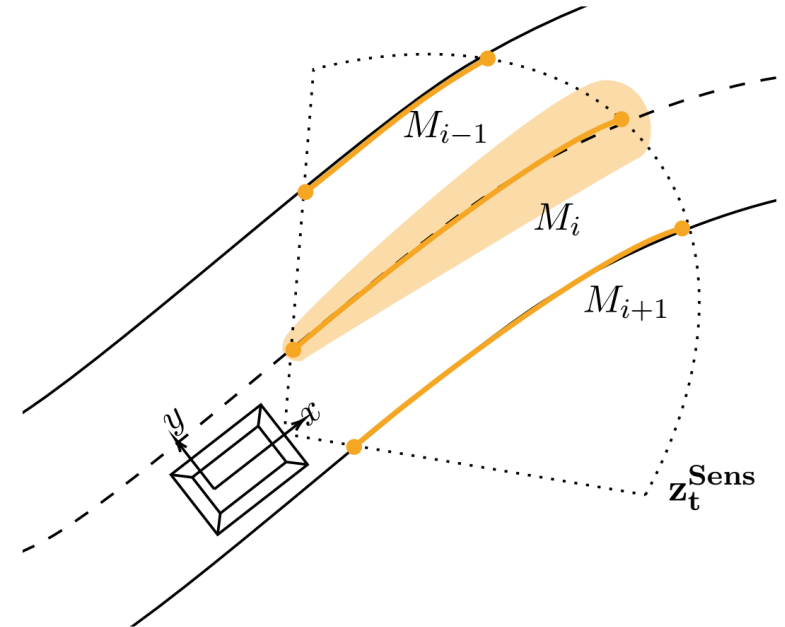
$$M_i = [c_0, c_1, c_2, c_3, x_{min}, x_{max}, \Sigma_P, M_{type}] \in \mathbf{z}_t^{\text{Sens}}$$

- Where $P(x)$ polynomial describes the curve:

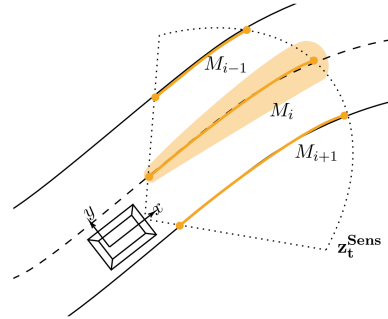
$$P(x) = c_0 + c_1x + c_2x^2 + c_3x^3, x \in [x_{min}, x_{max}]$$

- And Σ_P is the measurement error:

$$\Sigma_P = \begin{bmatrix} \sigma_{xx}^2 & & & & 0 & 0 \\ & \sigma_{c_0c_0}^2 & & & & 0 \\ & & \sigma_{c_1c_1}^2 & & & \\ 0 & & & \sigma_{c_2c_2}^2 & & \\ 0 & 0 & & & \sigma_{c_3c_3}^2 & \end{bmatrix}$$



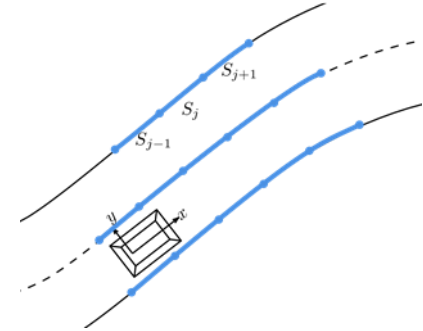
ROAD MODEL : PRO & CONS



Polynomial

Computation	Immediate (everywhere) ✓ ✓
Tracking evolution	Hard ✗
Descriptiveness	Limited ✗
Curvature-based navigation support	No ✗
Uncertainty representation	Coefficients ✗

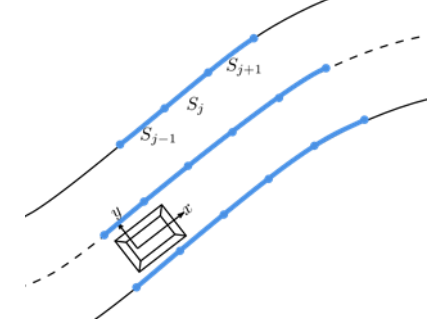
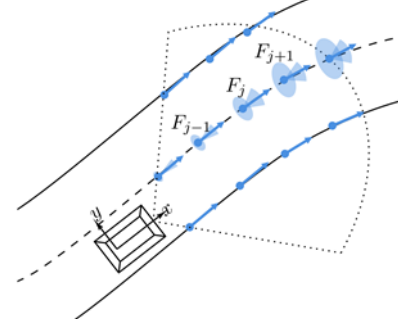
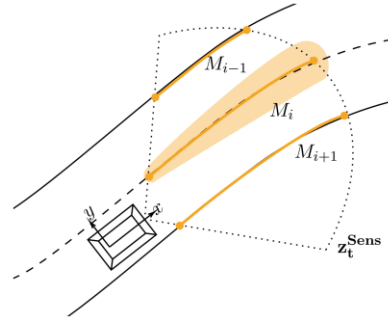
VS



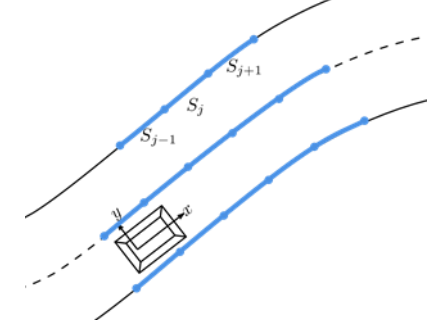
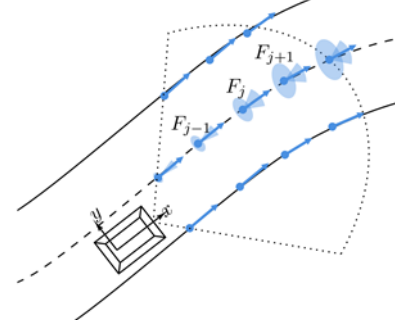
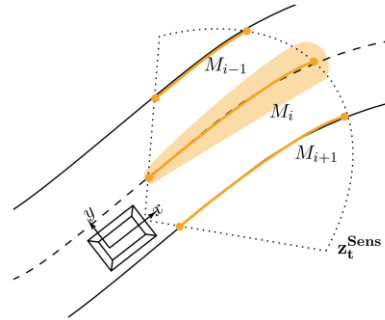
Clothoid-spline

Open integrals ✗ (eff. approx. method exist ✓)
Hard ✗
Complete (for road) ✓
Yes ✓
Clothoid params ✗

ROAD MODEL : PRO & CONS



	Polynomial	Road features	Clothoid-spline
Computation	Immediate (everywhere) ✓ ✓	Immediate (punctually) ✓ —	Open integrals ✗ (eff. approx. method exist ✓)
Tracking evolution	Hard ✗	Easy ✓	Hard ✗
Descriptiveness	Limited ✗	Complete (for any curve) ✓	Complete (for road) ✓
Curvature-based navigation support	No ✗	Discrete representation — (can turn into any curve ✓)	Yes ✓
Uncertainty representation	Coefficients ✗	Spatial ✓	Clothoid params ✗



	Polynomial	Road features	Clothoid-spline
Computation	Immediate (everywhere) ✓ ✓	Immediate (punctually) ✓ —	Open integrals ✗ (eff. approx. method exist ✓)
Tracking evolution	Hard ✗	Easy ✓	Hard ✗
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Curvature-based navigation support	No ✗	Discrete representation — (can turn into any curve ✓)	Yes ✓
Uncertainty representation	Coefficients ✗	Spatial ✓	Clothoid params ✗

IN

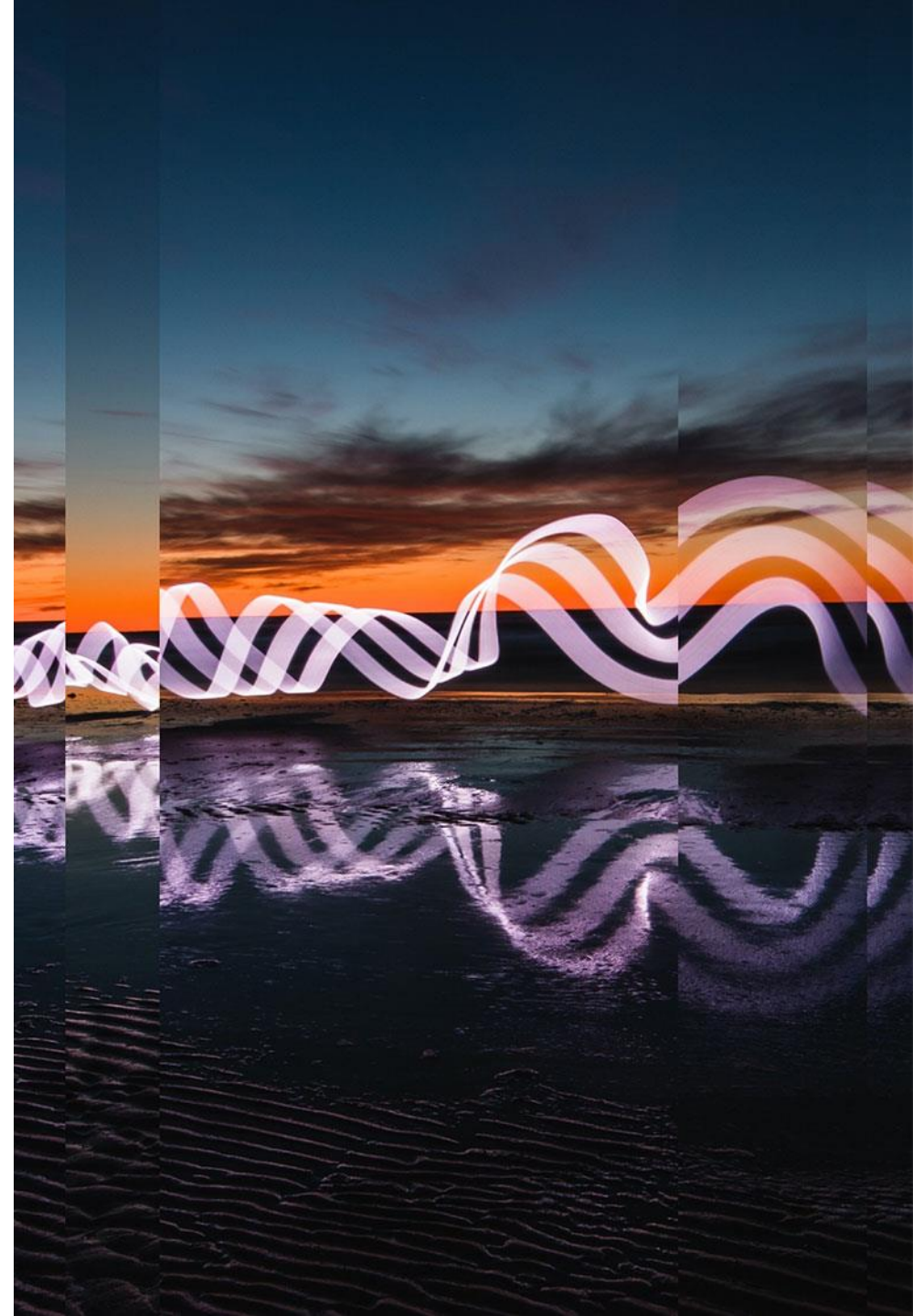
DURING estimation

OUT

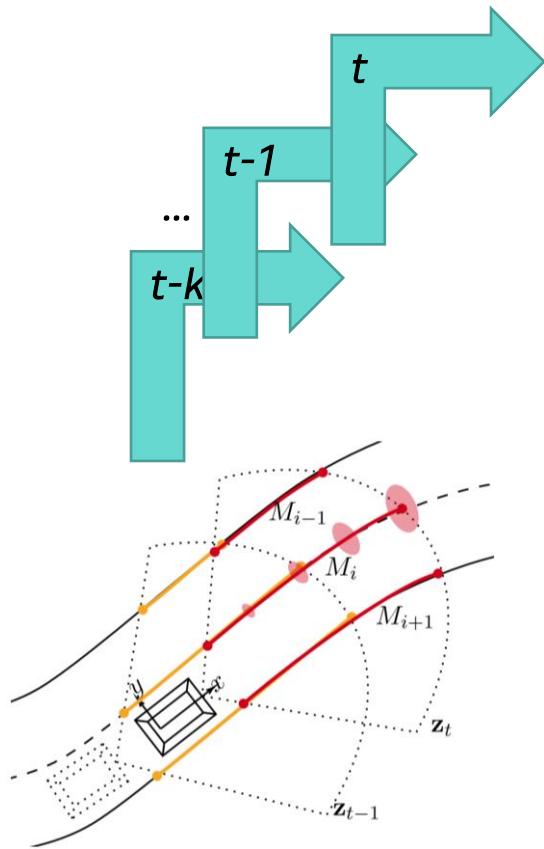
- 01** Thesis introduction
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- 03** Multi-sensor fusion for lane boundaries estimation
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03

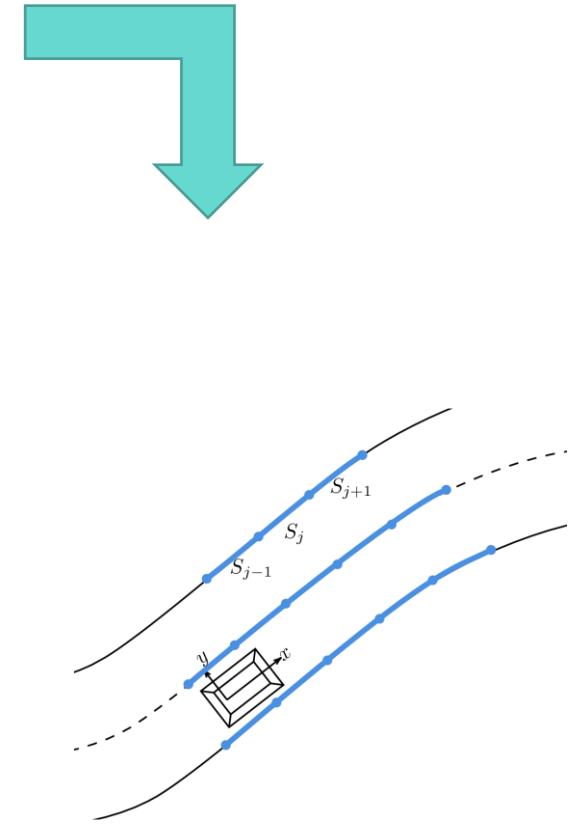
Multi-sensor fusion for lane boundaries estimation



PROPOSED SOLUTION : FEATURE-TRACKING

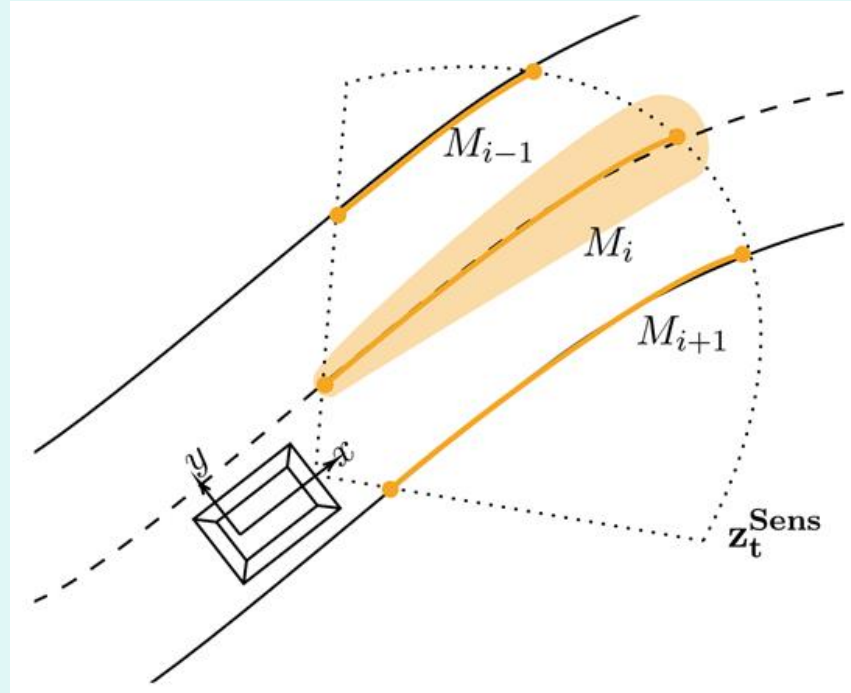


1. Initialization
2. Prediction
3. Association
4. Update
5. Output



PROPOSED SOLUTION : FEATURE-TRACKING

1. Initialization
2. Prediction
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4. Update
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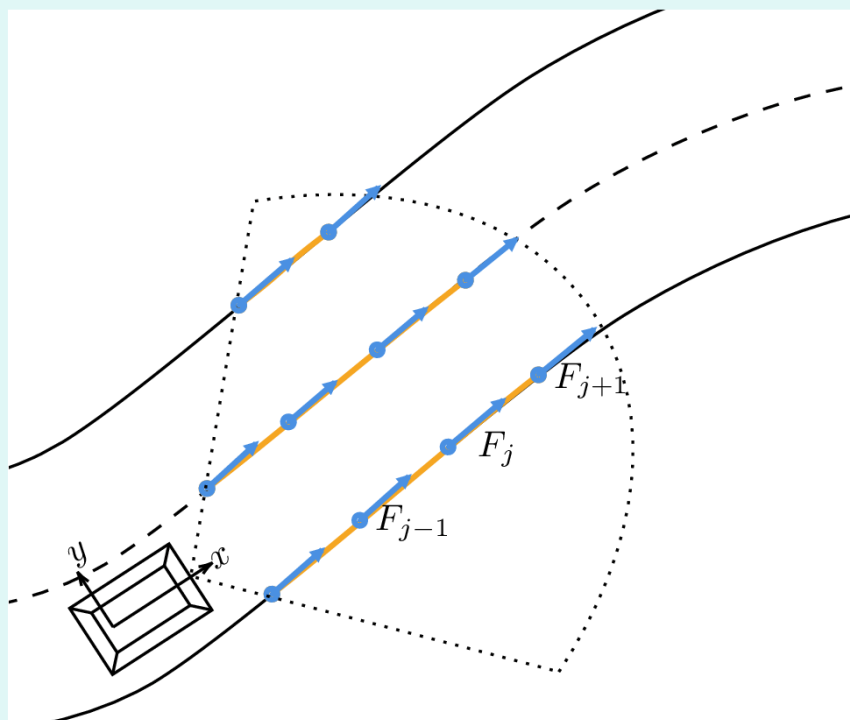
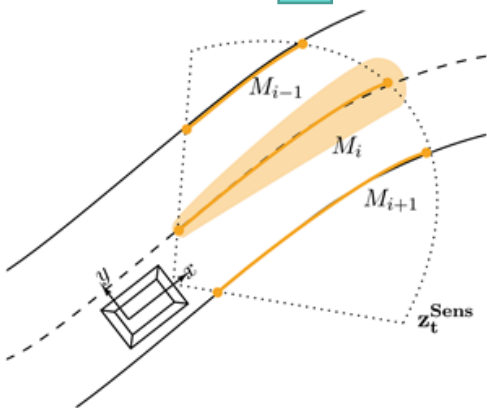
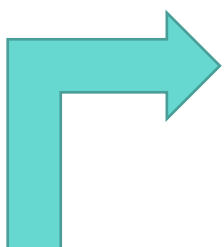
- First or non-associated measurements initialize distinct tracks for lane boundaries.
- Each measurement is delivered from the smart sensor in the form:

$$M_i = [c_0, c_1, c_2, c_3, x_{min}, x_{max}, \Sigma_P, M_{type}] \in \mathbf{z}_t^{\text{Sens}}$$

$$P(x) = c_0 + c_1x + c_2x^2 + c_3x^3, x \in [x_{min}, x_{max}]$$

PROPOSED SOLUTION : FEATURE-TRACKING

1. Initialization
2. Prediction
3. Association
4. Update
5. Output

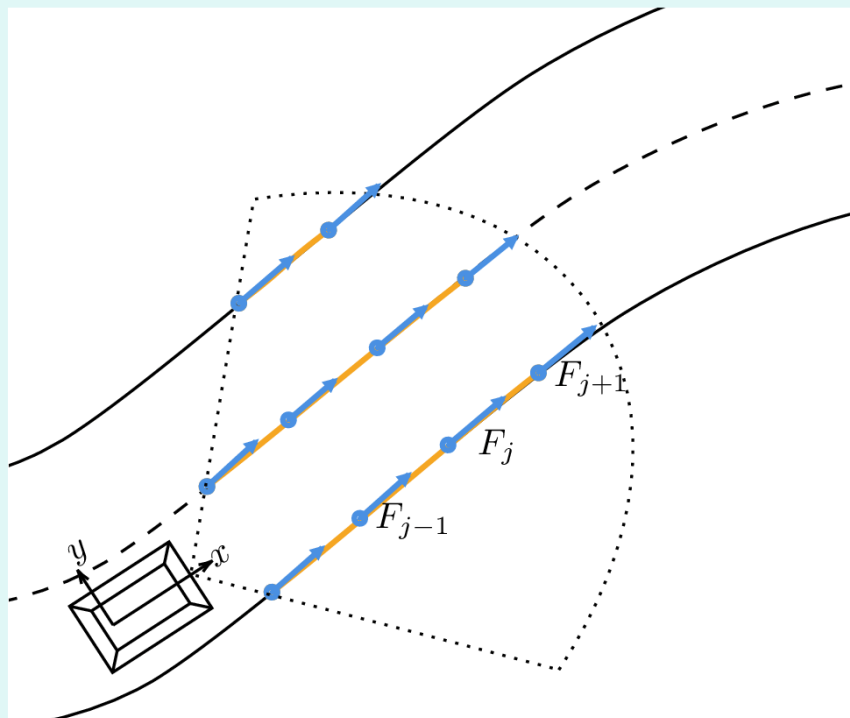
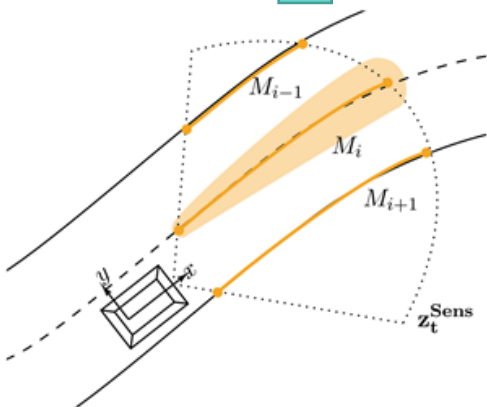
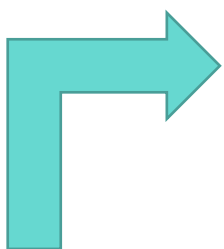


- Lane boundary tracks are collections of road features
- At constant interdistance, new features are sampled (according to the **sensor model**) as:

$$F_j = \begin{bmatrix} x_j \\ y_j \\ \theta_j \end{bmatrix} = \begin{bmatrix} x_j \\ P(x_j) \\ \arctan(P'(x_j)) \end{bmatrix} = \begin{bmatrix} x_j \\ c_0 + c_1x_j + c_2x_j^2 + c_3x_j^3 \\ \arctan(c_1 + 2c_2x_j + 3c_3x_j^2) \end{bmatrix}$$

PROPOSED SOLUTION : FEATURE-TRACKING

1. Initialization
2. **Prediction**
3. Association
4. Update
5. Output



- Ego-vehicle motion is estimated and delivered as :

$$\Delta Ego_t = [dx, dy, d\theta, \Sigma_E]$$

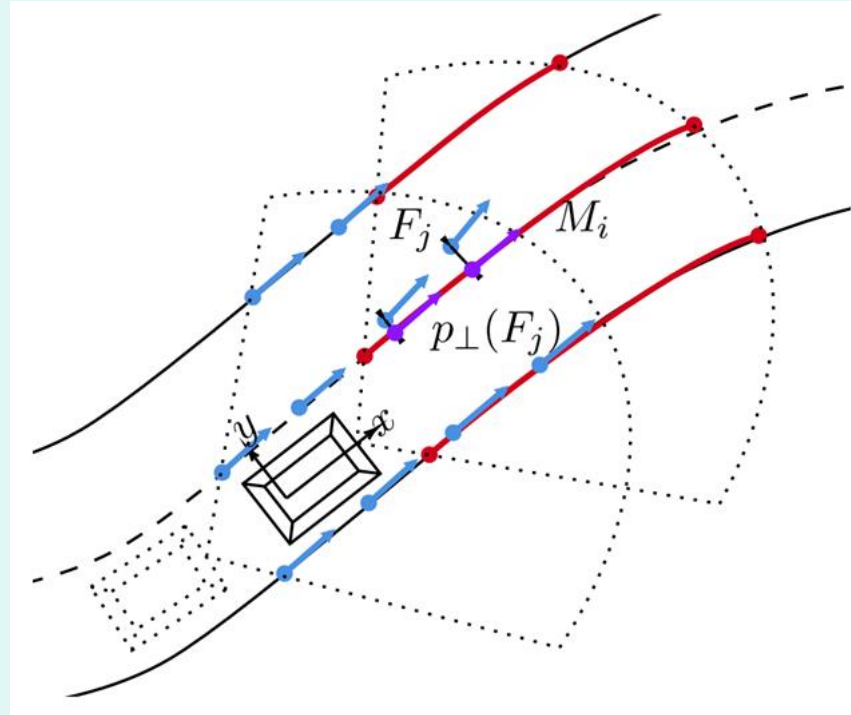
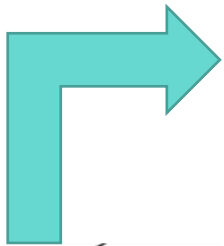
- After transformation into current reference frame, Kalman prediction step follows according to the trivial evolution model:

$$\mathbf{x}_t = \mathbf{x}_{t-1} + \mathbf{w}_t$$

$$\mathbf{w}_t \sim \mathcal{N}(0, \Sigma_E)$$

PROPOSED SOLUTION : FEATURE-TRACKING

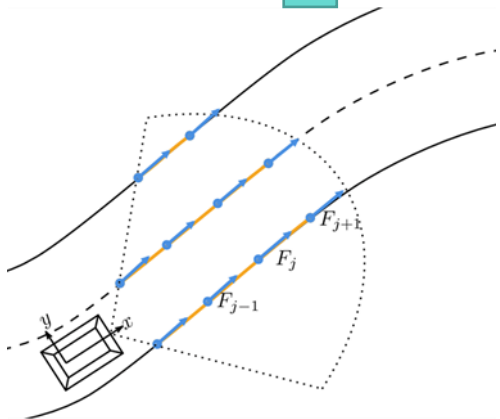
1. Initialization
2. Prediction
3. **Association**
4. Update
5. Output



- Existing features are projected onto measurements identifying Feature-to-Feature Mahalanobis distance:

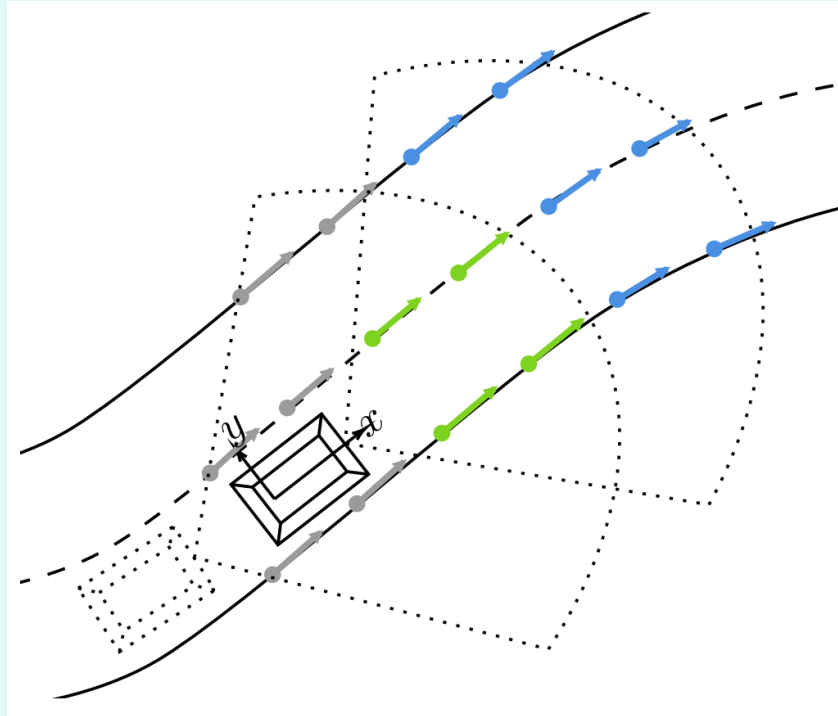
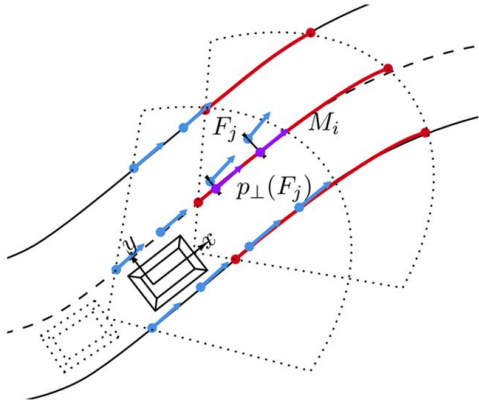
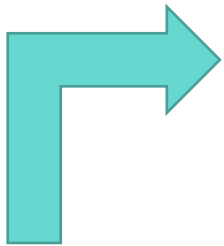
$$d(p_{\perp}(F_j), F_j) = \sqrt{(p_{\perp}(F_j) - F_j)^T (\Sigma_M(x_{\perp}, y_{\perp}) + \Sigma_F)^{-1} (p_{\perp}(F_j) - F_j)}$$

- Measure-to-track metric for GNN association: $d(M, C_i) = \max_{F_j \in C_i} d(p_{\perp}(F_j), F_j)$



PROPOSED SOLUTION : FEATURE-TRACKING

1. Initialization
2. Prediction
3. Association
4. **Update**
5. Output

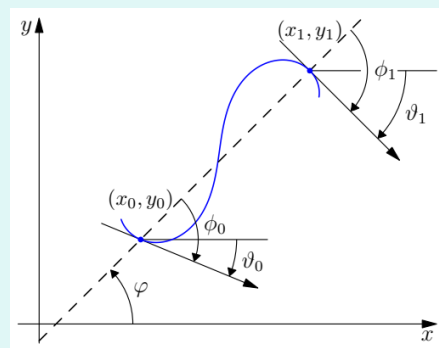
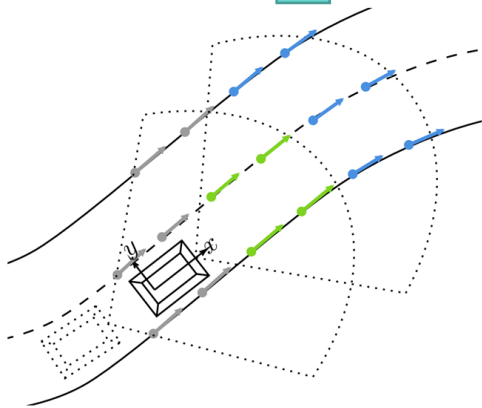
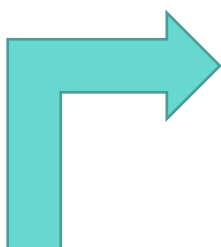


Three cases present depending on observability of road features :

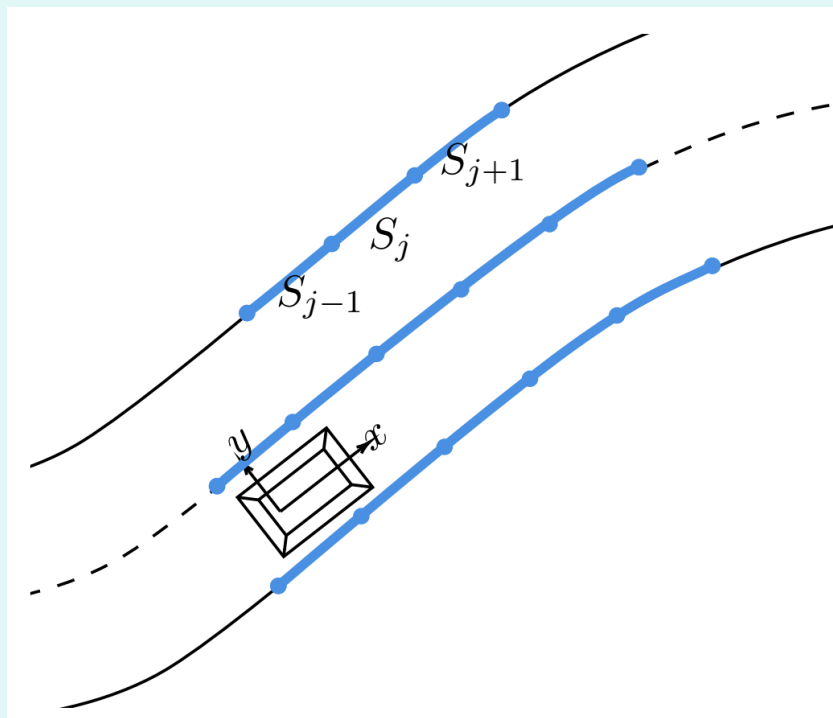
1. **Observed features** are updated following Kalman update step
2. **Unobserved features** can be suppressed if distant or obsolete
3. **Newly discovered features** (sampled at constant interdistance) extend existing tracks

PROPOSED SOLUTION : FEATURE-TRACKING

1. Initialization
2. Prediction
3. Association
4. Update
5. **Output**



$$S_j = [x_0, y_0, \psi_0, \kappa_0, \kappa_1, l, \Sigma_S]$$



- A road feature collection can be turned into clothoid-spline via interpolation
- Using the efficient interpolation method proposed in [6] between successive road features, the **resulting clothoid-spline attains G1-continuity** (heading angle of the curve is continuous all along its length) which makes it ideal for vehicle control

EXPERIMENTAL RESULTS

1. Development setup
2. Evaluation setup
3. On-board setup

EXPERIMENTAL RESULTS (1)

- Development setup



- Proprioceptives
- Smart FrontCam
30Hz, FoV: 53°x 120 m
- Smart AVM (4 cameras)
20Hz, FoV: 360°x 20 m

Sensors

Recording data



Re-playing data

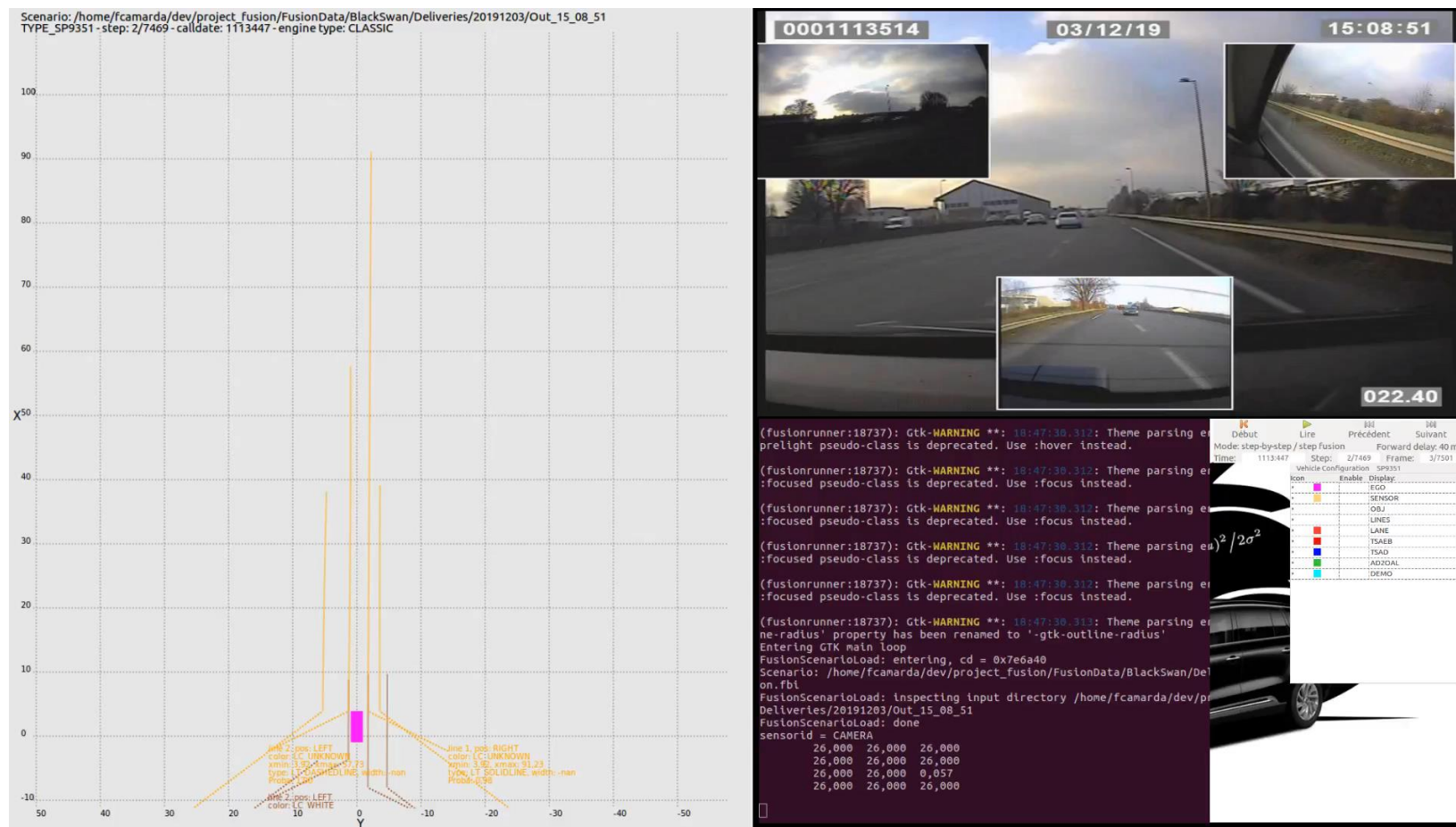
Fusionrunner environment

- Object tracking
- ...
- Ego-motion tracking
- Lane boundary tracking

Fusion results and context camera



- Execution in *Fusionrunner* environment



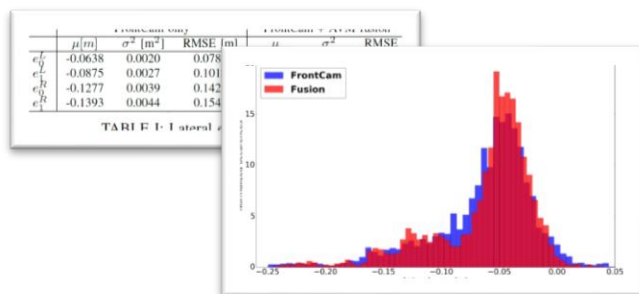
-  Ego-vehicle
-  Smart FrontCam measurements
-  Smart AVM measurements
-  Fusion result (road features)
-  Road features uncertainty
-  Fusion result (clothoid-spine)

EXPERIMENTAL RESULTS (2)

- Evaluation setup

- Performance indicators

Mean error at a given range, variance



- Lane-level ground truth

RTK localization + HD Map



Sensors

- Proprioceptives
- Smart FrontCam**
30Hz, FoV: 53°x120 m
- Smart AVM (4 cameras)**
20Hz, FoV: 360°x20 m

Recording data



Re-playing data

Fusionrunner environment

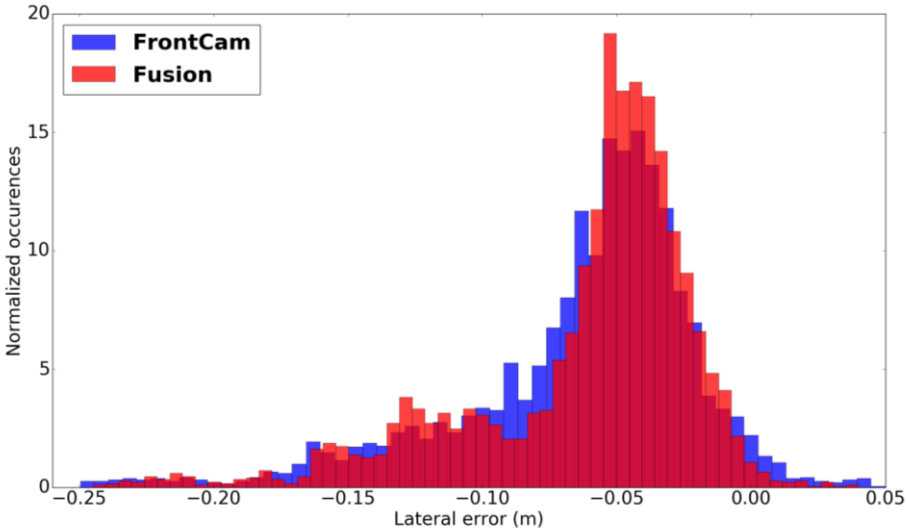
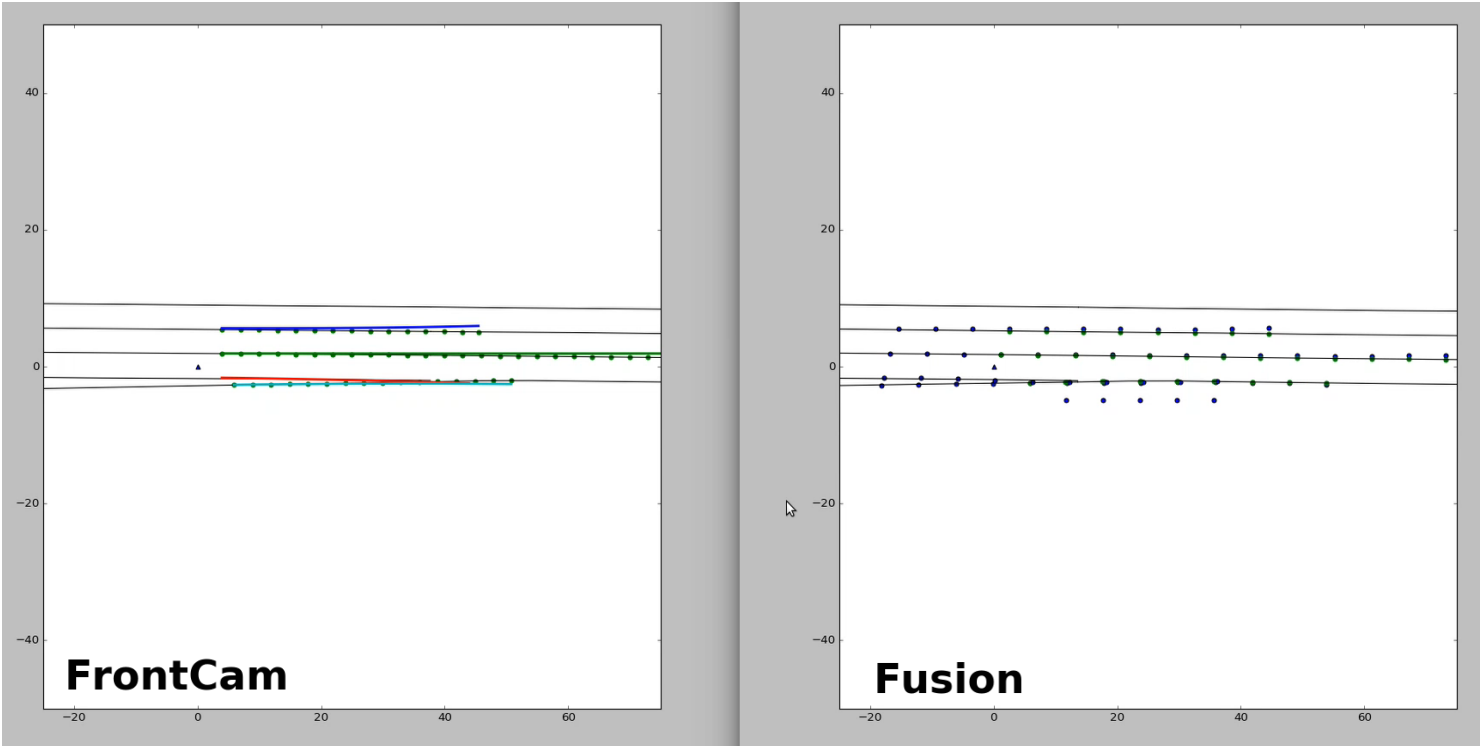
- Object tracking
- ...
- Ego-motion tracking
- Lane boundary tracking

VS

03 MULTI-SENSOR FUSION FOR LANE BOUNDARIES ESTIMATION

EXPERIMENTAL RESULTS (2)

- FrontCam only vs FrontCam+AVM Fusion
 - Lateral error at given range is computed w.r.t. lane-level GT
 - Fusion smoothing effect reflects in lateral error at 0m distribution

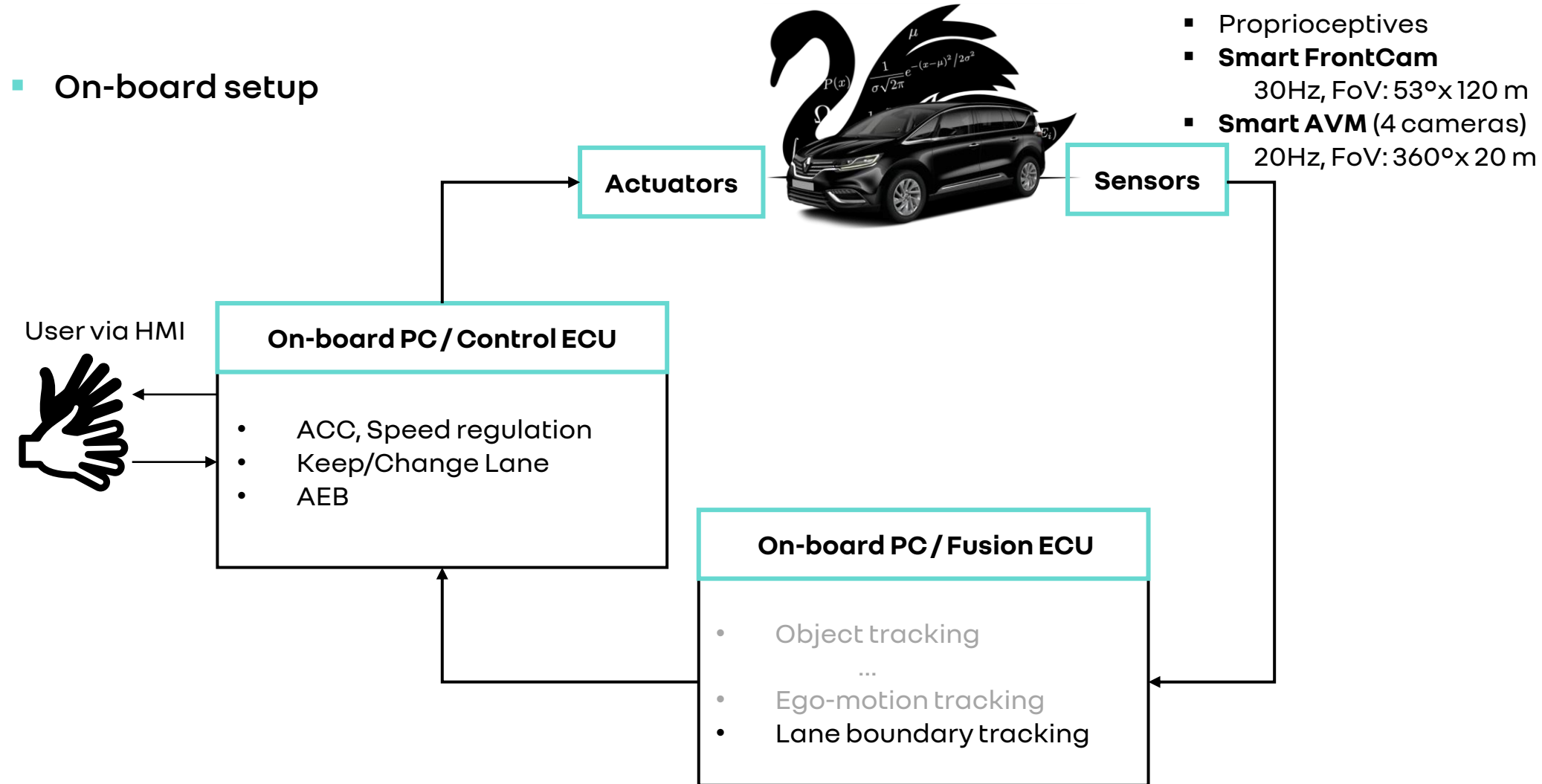


	FrontCam only			FrontCam + AVM fusion		
	$\mu[m]$	$\sigma^2[m^2]$	RMSE [m]	μ	σ^2	RMSE
e_0^L	-0.0638	0.0020	0.0781	-0.0620	0.0019	0.0755
e_1^L	-0.0875	0.0027	0.1018	-0.0773	0.0022	0.0906
e_0^R	-0.1277	0.0039	0.1421	-0.1018	0.0024	0.1131
e_1^R	-0.1393	0.0044	0.1543	-0.1254	0.0037	0.1394

TABLE I: Lateral error benchmark

EXPERIMENTAL RESULTS (3)

- On-board setup



EXPERIMENTAL RESULTS (3)



1. ACC is activated, **Keep lane**
2. Lane boundaries are detected by FrontCam + AVM and fused
3. Left turn signal is activated, **Change lane (to left)**
4. Back to **Keep lane**
5. Right turn signal is activated, **Change lane (to right)**

- Change Lane based FrontCam + AVM : successful on-board execution ✓

SECTION CONCLUSIONS

Multi-sensor architecture for tracking of lane boundaries has been introduced and validated

Can support potentially any multi-modal smart sensor set, providing **redundancy** and **perception diversity**

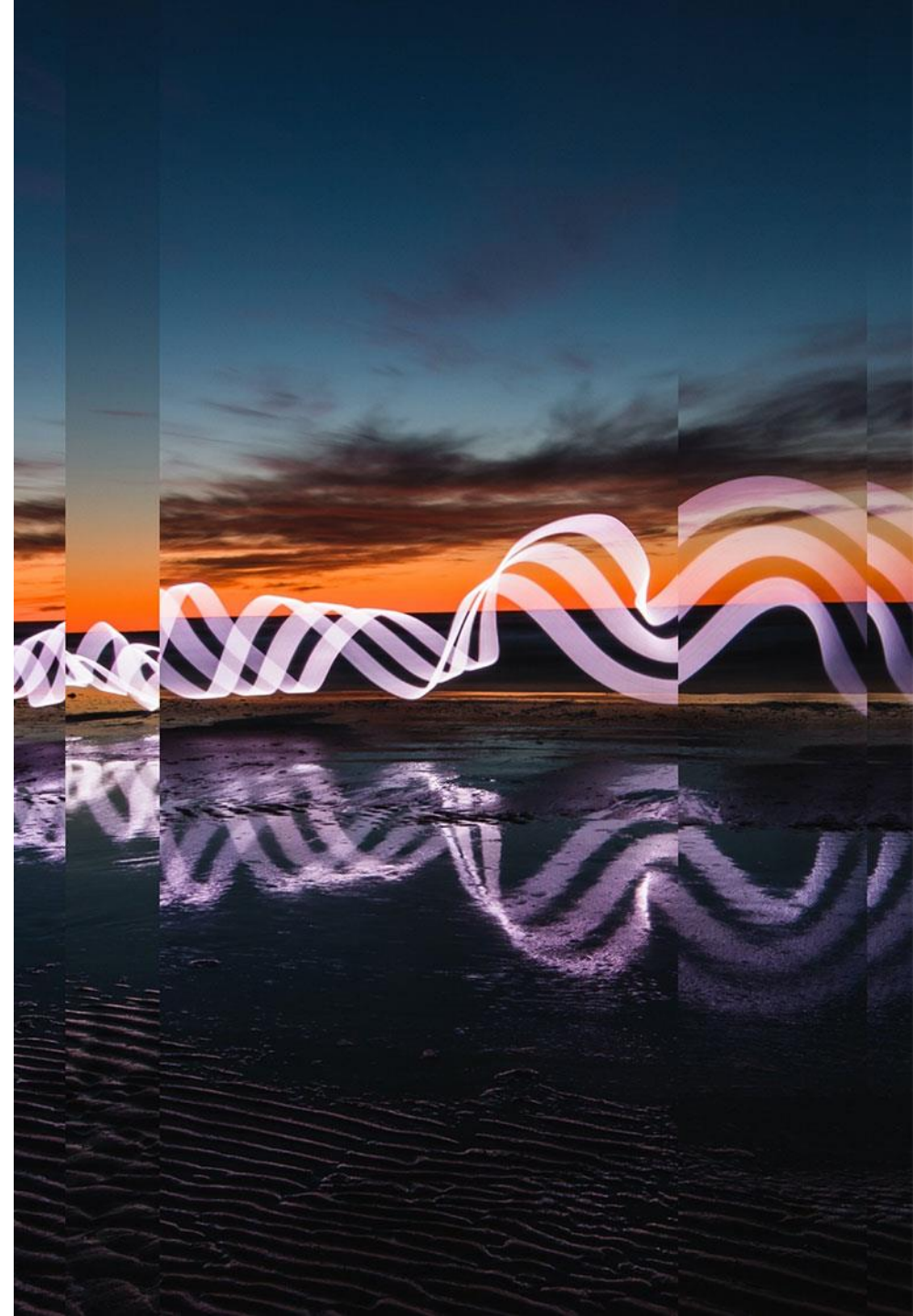
Real-time implementation and on-board experiments confirm **exploitability** in quasi-industrial use cases

✓ Work accepted as contributed paper at :
2020 IEEE Intelligent Vehicles Symposium (IV 2020)

- 01** Thesis introduction
- 02** Problem formulation
- 03** Multi-sensor fusion for lane boundaries estimation
- 04** Map-aided multi-sensor fusion for lane boundaries estimation
- 05** Conclusions

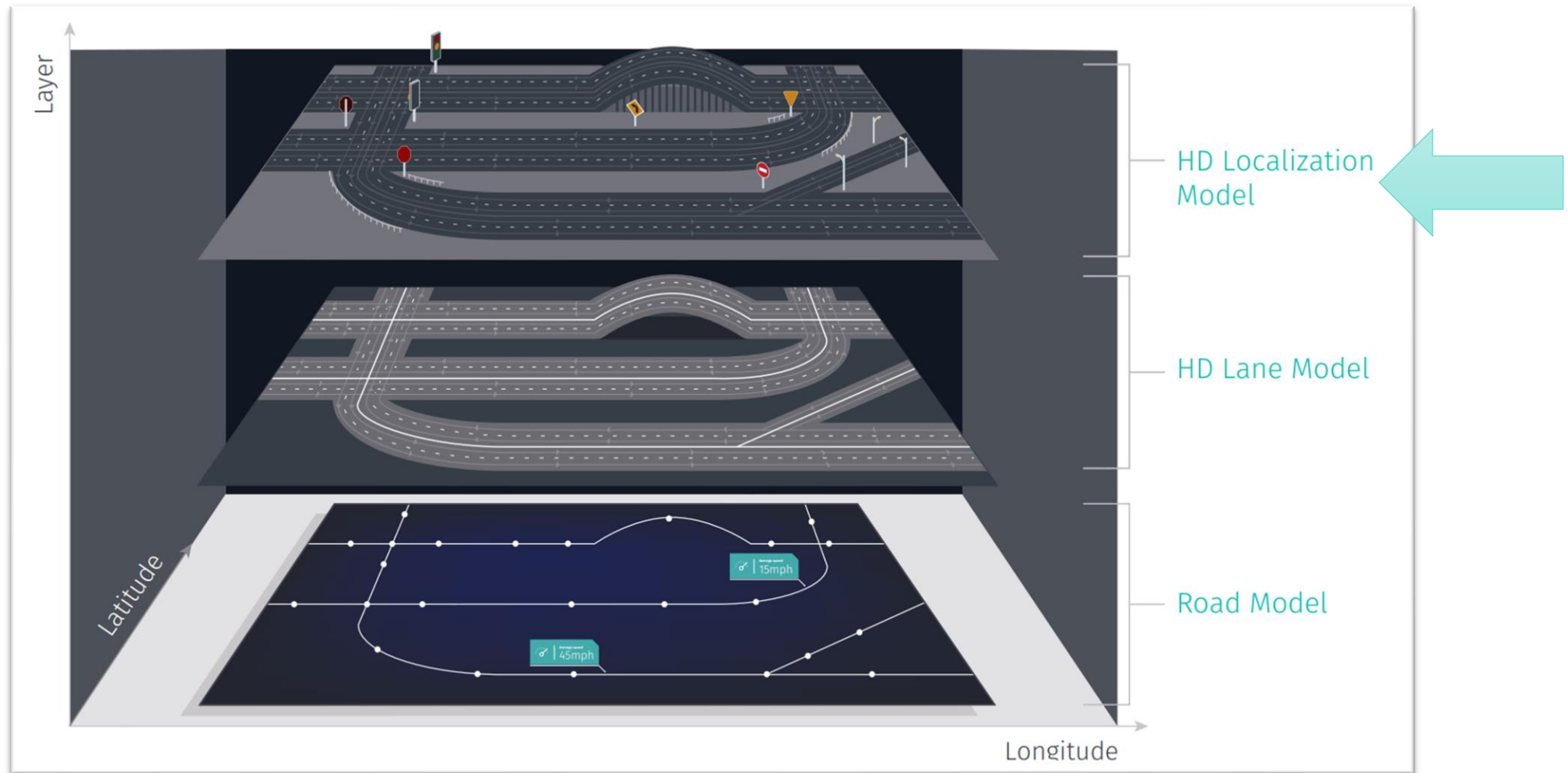
04

Map-aided multi-sensor fusion for lane boundaries estimation



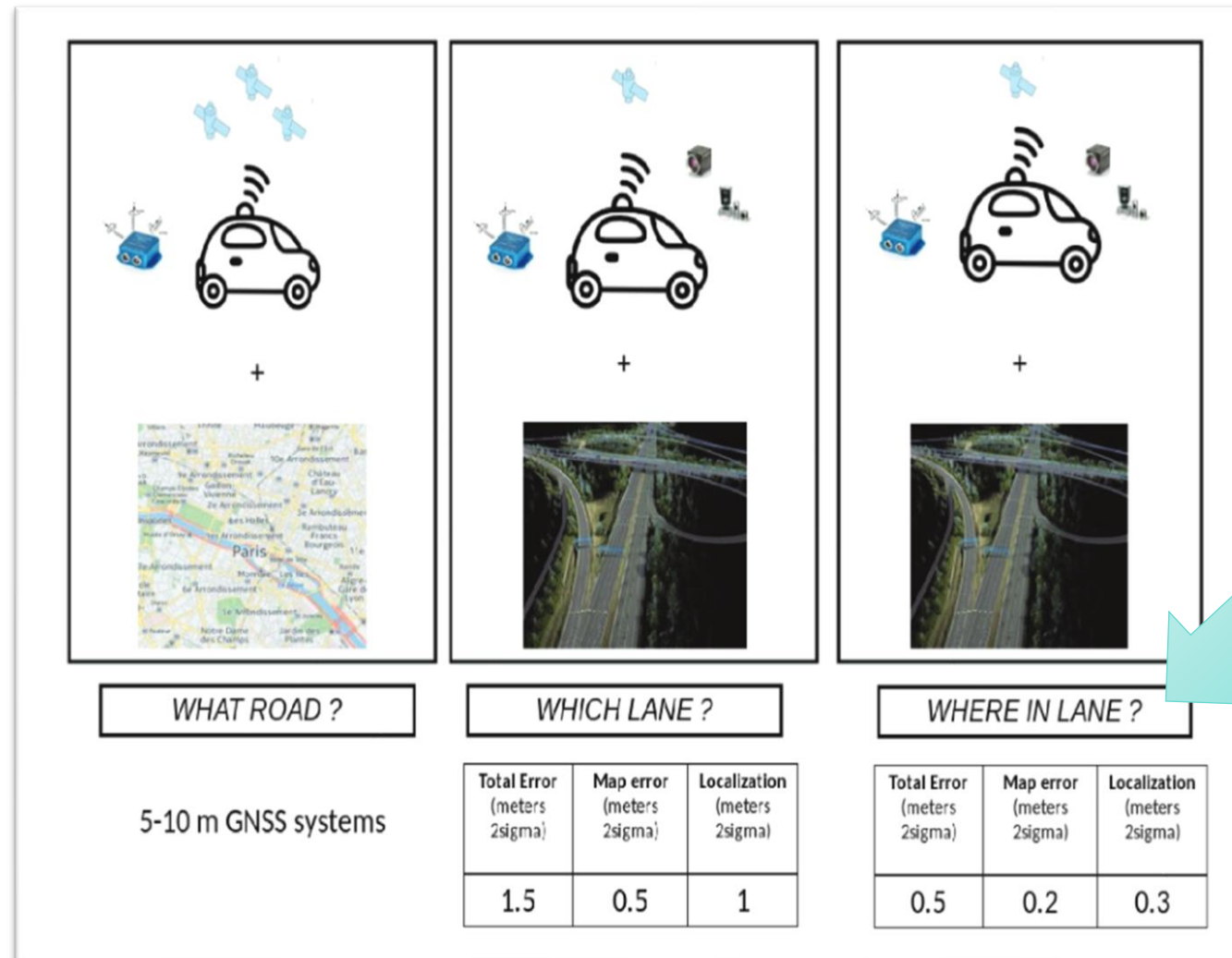
MAP-PROVIDERS : STATE OF THE ART

■ Mapping and Localization

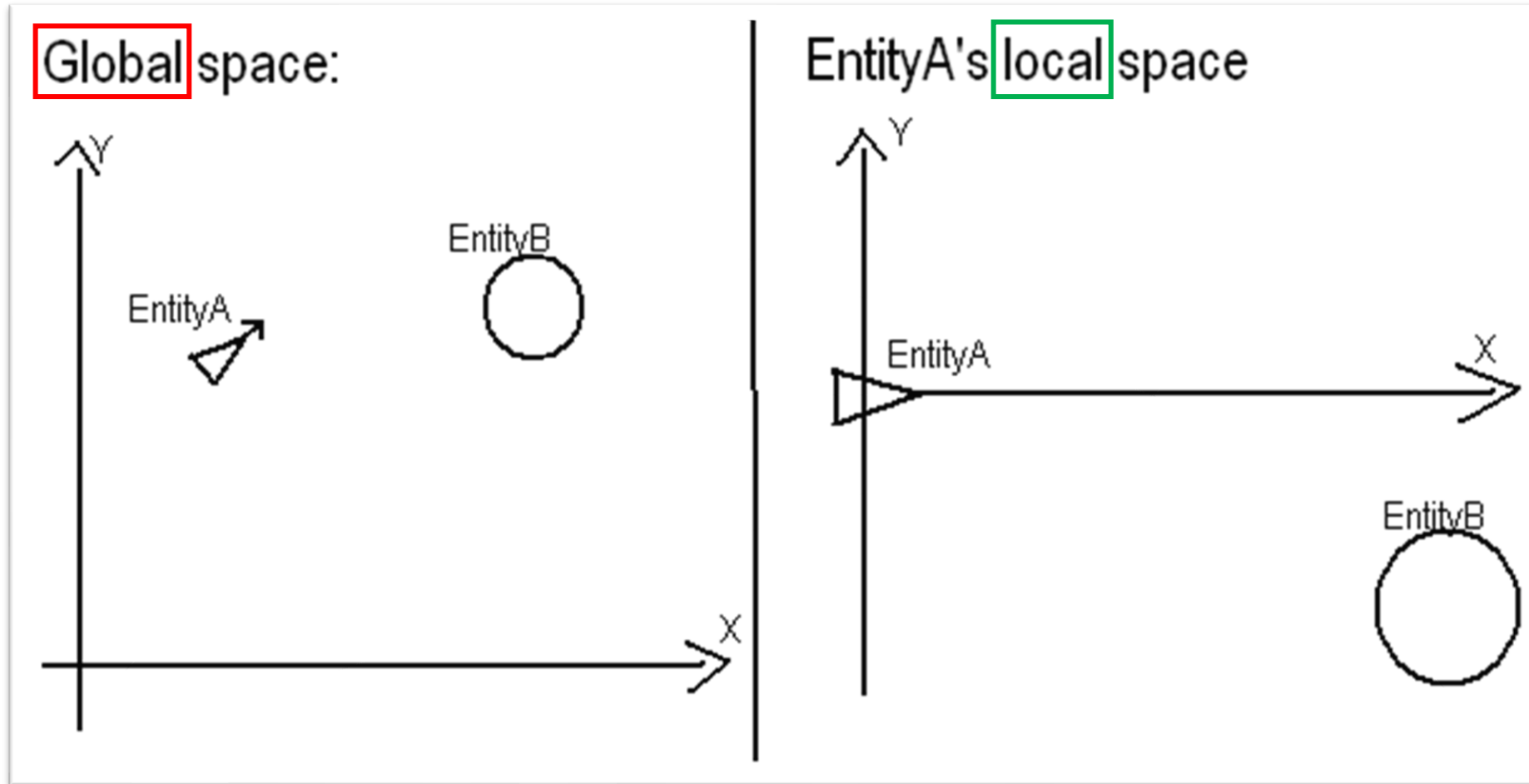


MAP-PROVIDERS : STATE OF THE ART

■ Mapping and Localization



MAP-PROVIDER MODEL : GLOBAL AND LOCAL FRAME



- *EntityA* is ego-vehicle – *EntityB* is a map-node

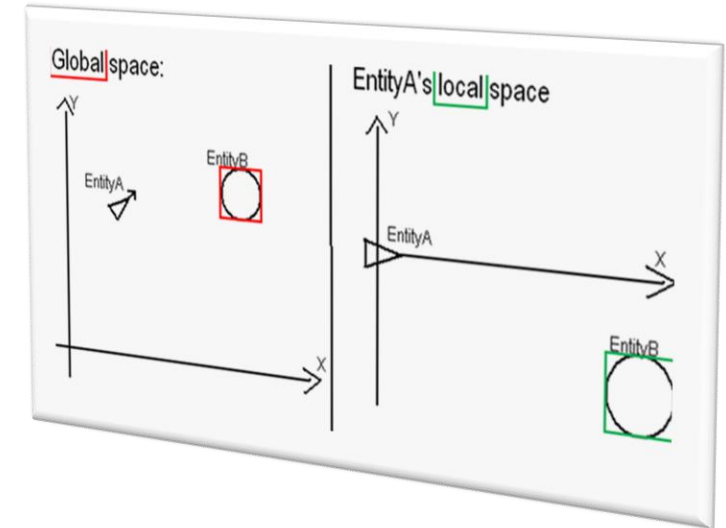
MAP-PROVIDER MODEL : UNCERTAINTY REPRESENTATION

- Map-node in the global frame

$$\boxed{O}\mathbf{X}_i = \begin{bmatrix} {}^O x_i \\ {}^O y_i \end{bmatrix}$$

- Map-node in the local frame

$$\boxed{M}\mathbf{X}_i = \begin{bmatrix} {}^M x_i \\ {}^M y_i \end{bmatrix} = {}^M\mathbf{R}_O \left(\begin{bmatrix} {}^O x_i \\ {}^O y_i \end{bmatrix} - \begin{bmatrix} {}^O x_M \\ {}^O y_M \end{bmatrix} \right) = f({}^O\mathbf{X}_M, \theta, {}^O\mathbf{X}_i)$$



MAP-PROVIDER MODEL : UNCERTAINTY REPRESENTATION

- Uncertainty of map-node in the global frame

$$Var(\overset{O}{\mathbf{X}}_i) = Var(\overset{O}{\mathbf{X}}_{Map}) \forall i = 1..N_i$$

- Uncertainty of map-node in the local frame

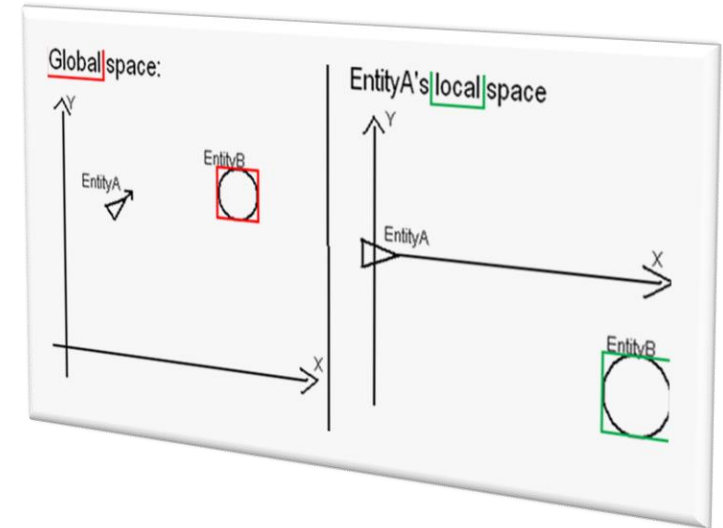
$$Var(\overset{M}{\mathbf{X}}_i) = \begin{bmatrix} \frac{\partial f}{\partial \overset{O}{\mathbf{X}}_5} \end{bmatrix} \begin{bmatrix} \overset{O}{\Sigma}_M & \mathbf{0} \\ \mathbf{0} & Var(\overset{O}{\mathbf{X}}_i) \end{bmatrix} \begin{bmatrix} \frac{\partial f}{\partial \overset{O}{\mathbf{X}}_5} \end{bmatrix}^T$$

Takes into account both mapping and localization error! ✓

- where:

$$\begin{bmatrix} \frac{\partial f}{\partial \overset{O}{\mathbf{X}}_5} \end{bmatrix} = \begin{bmatrix} -\cos(\theta) & -\sin(\theta) & \overset{M}{y}_i & \cos(\theta) & \sin(\theta) \\ \sin(\theta) & -\cos(\theta) & -\overset{M}{x}_i & -\sin(\theta) & \cos(\theta) \end{bmatrix}$$

Do not depend on global coordinates ! Can be computed after map-provider delivered ✓



MAP-PROVIDERS : UNCERTAINTY REPRESENTATION

Definitions:

$${}^O\mathbf{X}_i = \begin{bmatrix} {}^Ox_i \\ {}^Oy_i \end{bmatrix}$$

$$\text{Var}({}^O\mathbf{X}_i) = \text{Var}({}^O\mathbf{X}_{Map}) \forall i = 1..N_i$$

$${}^M\mathbf{R}_O = {}^O\mathbf{R}_M^T = \begin{bmatrix} \cos(\theta) & \sin(\theta) \\ -\sin(\theta) & \cos(\theta) \end{bmatrix}$$

$${}^O\Sigma_M = \text{Var}\left(\begin{bmatrix} {}^Ox_M \\ {}^Oy_M \\ \theta \end{bmatrix}\right)$$

$${}^M\mathbf{X}_i = \begin{bmatrix} {}^Mx_i \\ {}^My_i \end{bmatrix} = {}^M\mathbf{R}_O \left(\begin{bmatrix} {}^Ox_i \\ {}^Oy_i \end{bmatrix} - \begin{bmatrix} {}^Ox_M \\ {}^Oy_M \end{bmatrix} \right) = f({}^O\mathbf{X}_M, \theta, {}^O\mathbf{X}_i)$$

$${}^O\mathbf{X}_5 = ({}^O\mathbf{X}_M, \theta, {}^O\mathbf{X}_i)$$

Then:

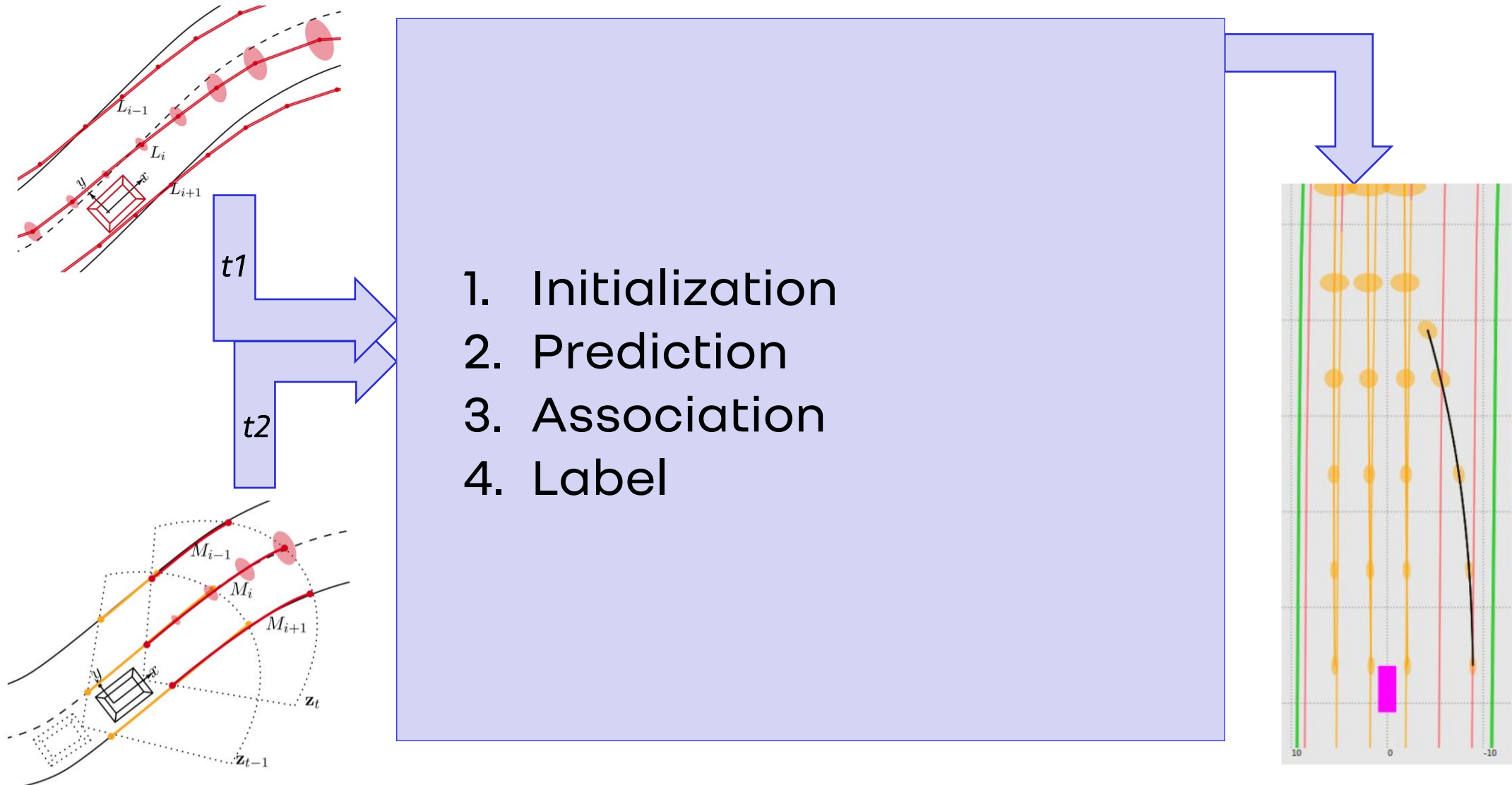
$$f({}^O\mathbf{X}_M, \theta, {}^O\mathbf{X}_i) = \begin{bmatrix} ({}^Ox_i - {}^Ox_M) \cos(\theta) + ({}^Oy_i - {}^Oy_M) \sin(\theta) \\ -({}^Ox_i - {}^Ox_M) \sin(\theta) + ({}^Oy_i - {}^Oy_M) \cos(\theta) \end{bmatrix}$$

$$\left[\frac{\partial f}{\partial {}^O\mathbf{X}_5} \right] = \begin{bmatrix} -\cos(\theta) & -\sin(\theta) & -({}^Ox_i - {}^Ox_M) \sin(\theta) + ({}^Oy_i - {}^Oy_M) \cos(\theta) & \cos(\theta) & \sin(\theta) \\ \sin(\theta) & -\cos(\theta) & -({}^Ox_i - {}^Ox_M) \cos(\theta) - ({}^Oy_i - {}^Oy_M) \sin(\theta) & -\sin(\theta) & \cos(\theta) \end{bmatrix}$$

$$= \begin{bmatrix} -\cos(\theta) & -\sin(\theta) & {}^My_i & \cos(\theta) & \sin(\theta) \\ \sin(\theta) & -\cos(\theta) & -{}^Mx_i & -\sin(\theta) & \cos(\theta) \end{bmatrix}$$

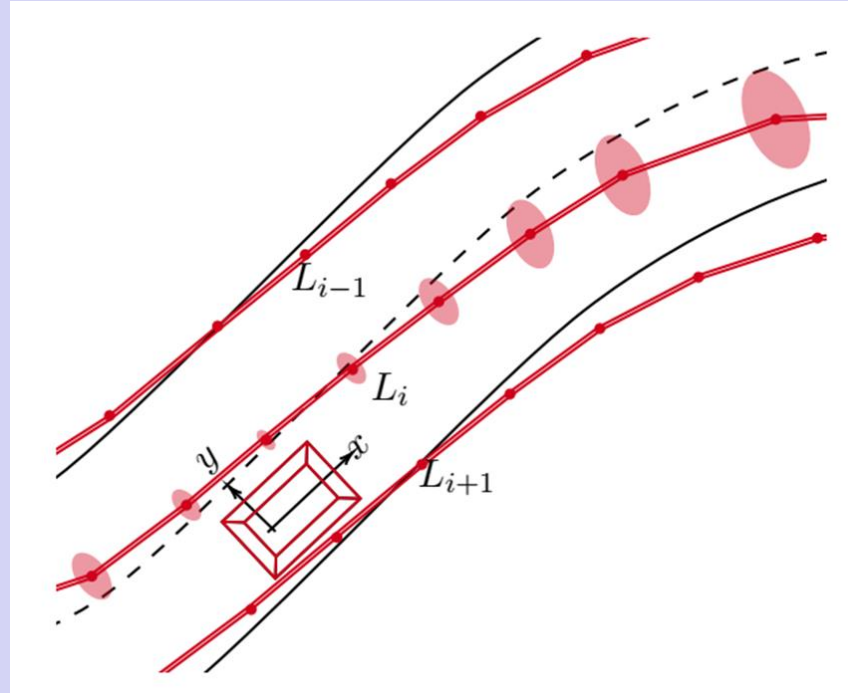
$$\text{Var}({}^M\mathbf{X}_i) = \left[\frac{\partial f}{\partial {}^O\mathbf{X}_5} \right] \begin{bmatrix} {}^O\Sigma_M & \mathbf{0} \\ \mathbf{0} & \text{Var}({}^O\mathbf{X}_i) \end{bmatrix} \left[\frac{\partial f}{\partial {}^O\mathbf{X}_5} \right]^T$$

PROPOSED SOLUTION: LANE BOUNDARIES ASSOCIATION



PROPOSED SOLUTION : LANE BOUNDARIES ASSOCIATION

1. Initialization
2. Prediction
3. Association
4. Label



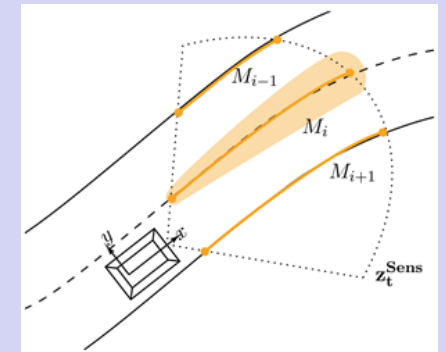
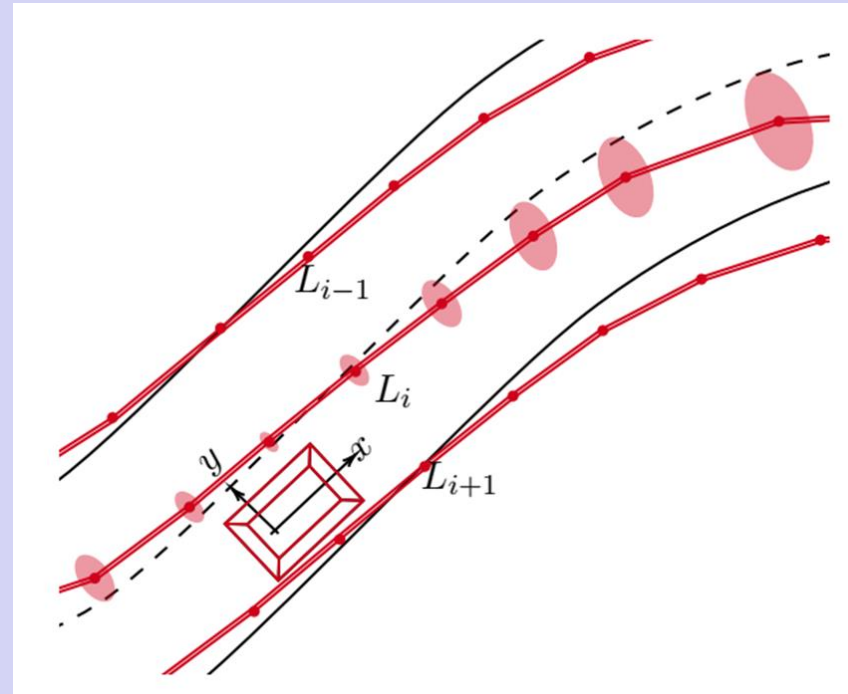
- Road feature are initialized from map-provider delivery and according to mapping and localization error model:

$$F_j = [x_j, y_j, \theta_j, \Sigma_F]$$

$$\Sigma_F = Var({}^M \mathbf{X}_i)$$

PROPOSED SOLUTION : LANE BOUNDARIES ASSOCIATION

1. Initialization
- 2. Prediction**
3. Association
4. Label



- Predict the status of the (map-provided) road features according to ego-movement estimation:

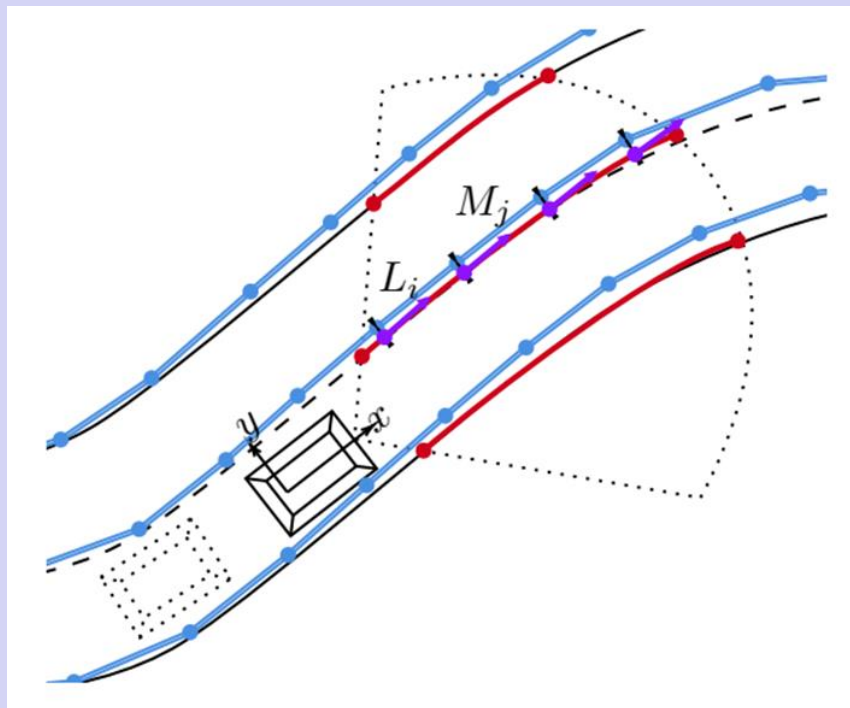
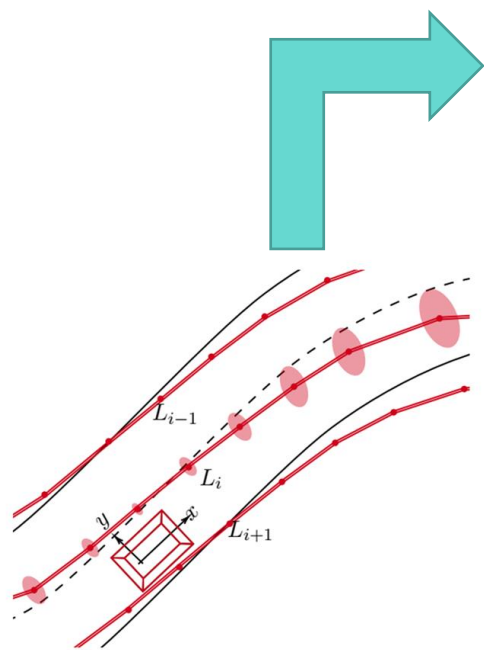
$$\Delta Ego_t = [dx, dy, d\theta, \Sigma_E]$$

$$\mathbf{w}_t \sim \mathcal{N}(0, \Sigma_E)$$

- Up to the latest smart sensor delivery measure date

PROPOSED SOLUTION : LANE BOUNDARIES ASSOCIATION

1. Initialization
2. Prediction
3. **Association**
4. Label



- Map-nodes (as road features) are projected onto measurements identifying Feature-to-Feature Mahalanobis distance:

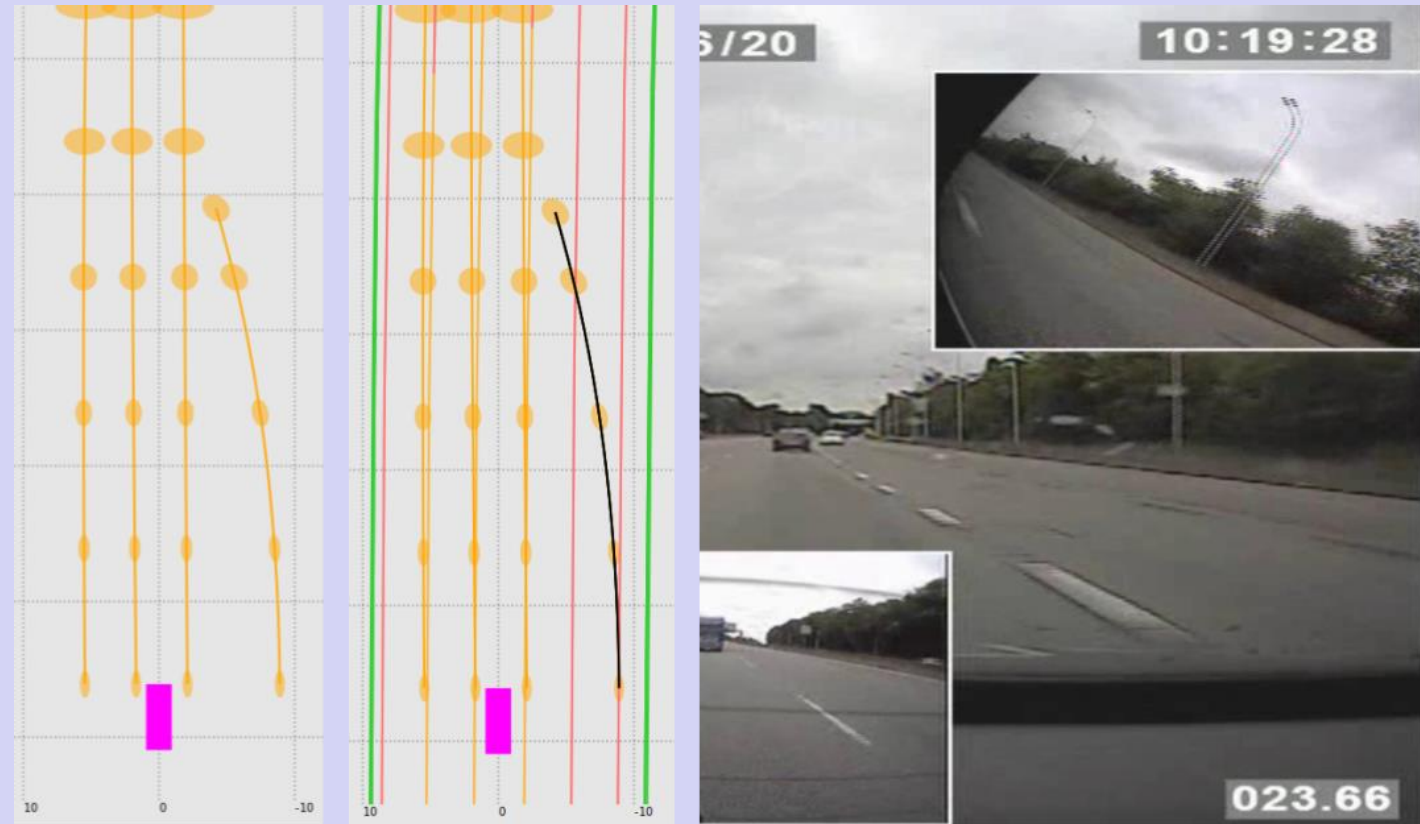
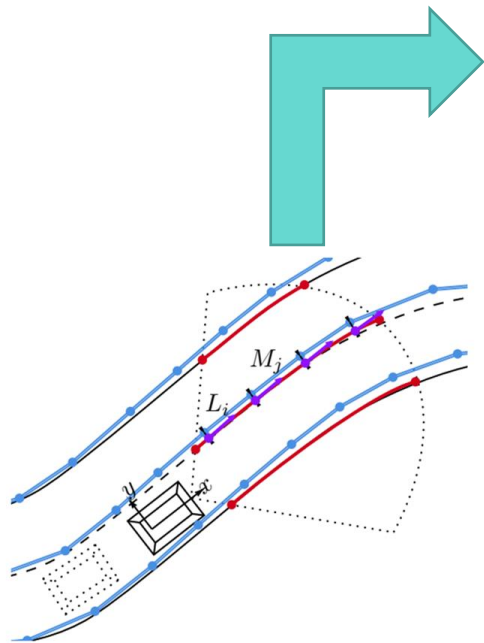
$$d^2(p_{\perp}(F_j), F_j) = (p_{\perp}(F_j) - F_j)^T ({}^M \Sigma_F + Var({}^M \mathbf{X}_i))^{-1} (p_{\perp}(F_j) - F_j)$$

- M to L distance metric for GNN association:

$$d(M, L) = \max_{F_j \in L} d(p_{\perp}(F_j), F_j)$$

PROPOSED SOLUTION : LANE BOUNDARIES ASSOCIATION

1. Initialization
2. Prediction
3. Association
4. **Label**



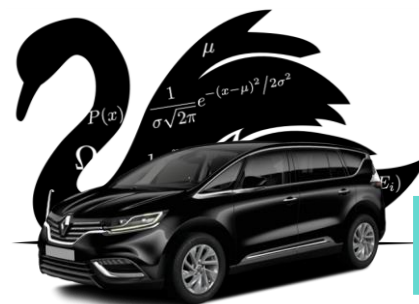
- The HD-map is supposed to be complete of all detectable lane boundaries
- Then Non-Associated smart sensor measurements are **labeled** as False Positives

EXPERIMENTAL RESULTS

1. Development setup
2. Application for false positives detection
3. Scoring for multiple hypotheses of ego-vehicle localization

EXPERIMENTAL RESULTS

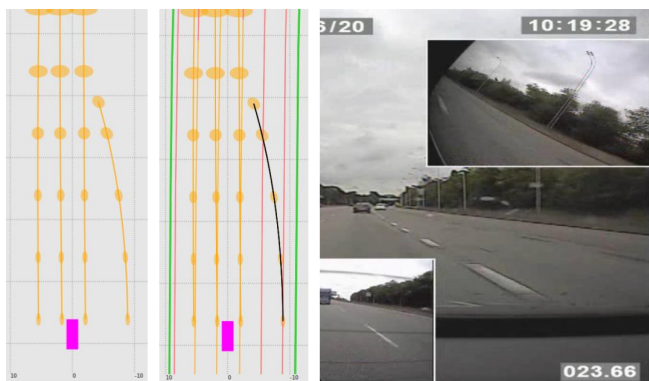
- Development setup



Sensors

- Proprioceptives    
- eHorizon**
1Hz, FoV: 360°x 200 m
- Smart FrontCam**
30Hz, FoV: 53°x 120 m
- Smart AVM (4 cameras)**
20Hz, FoV: 360°x 20 m

Fusion results and context camera



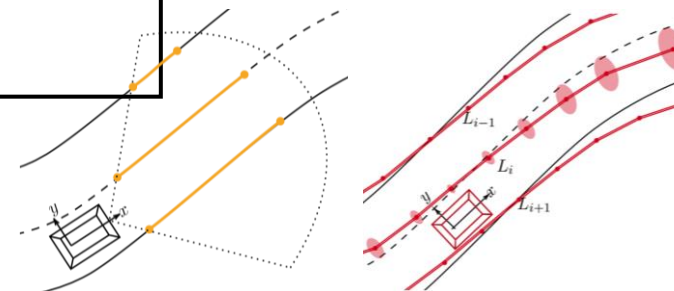
Fusionrunner environment

- Object tracking
- ...
- Ego-motion tracking
- Lane boundary tracking

Recording data



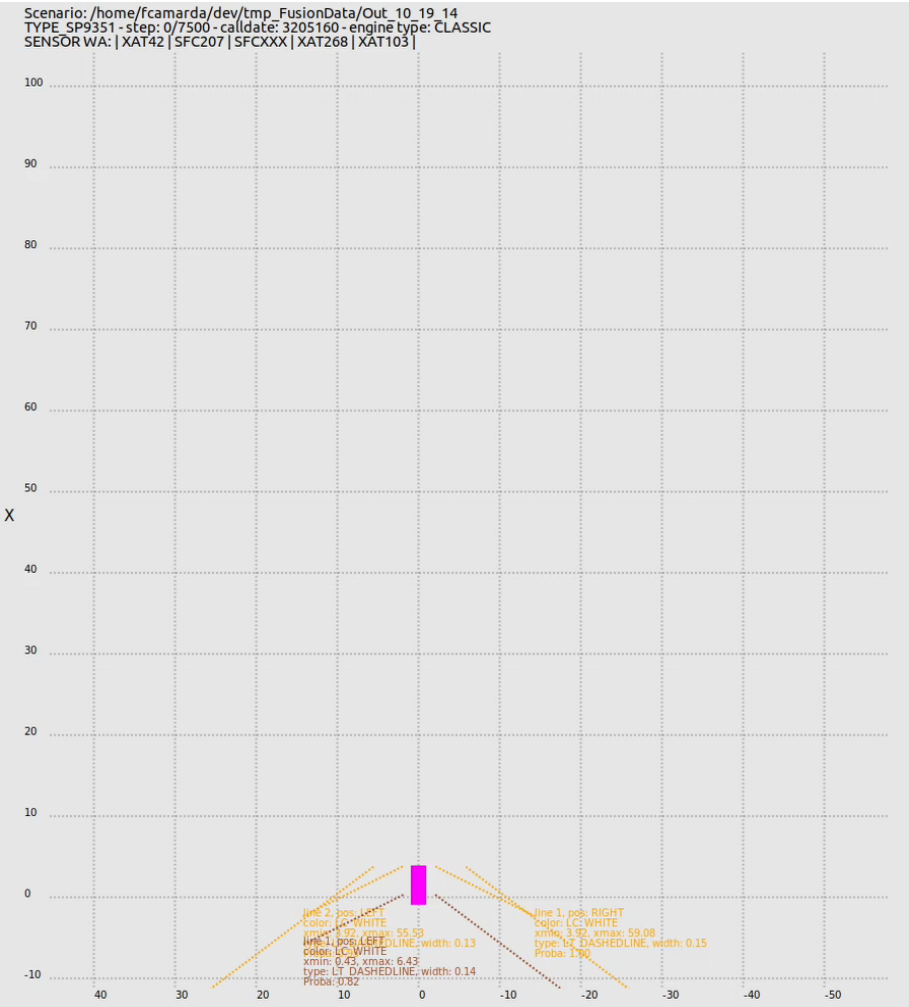
Re-playing data



04 MAP-AIDED MULTI-SENSOR FUSION FOR LANE BOUNDARIES ESTIMATION

EXPERIMENTAL RESULTS

- Execution in *Fusionrunner* environment : qualitative evaluation



-  Ego-vehicle
-  Other vehicles
-  Map lane b. (road markings)
-  Map lane b. (barriers)
-  Map lane b. associated to Smart FrontCam measurements
-  Map lane b. associated to Smart AVM measurements
-  Road features uncertainty
-  Non-associated Smart Sensor measurements

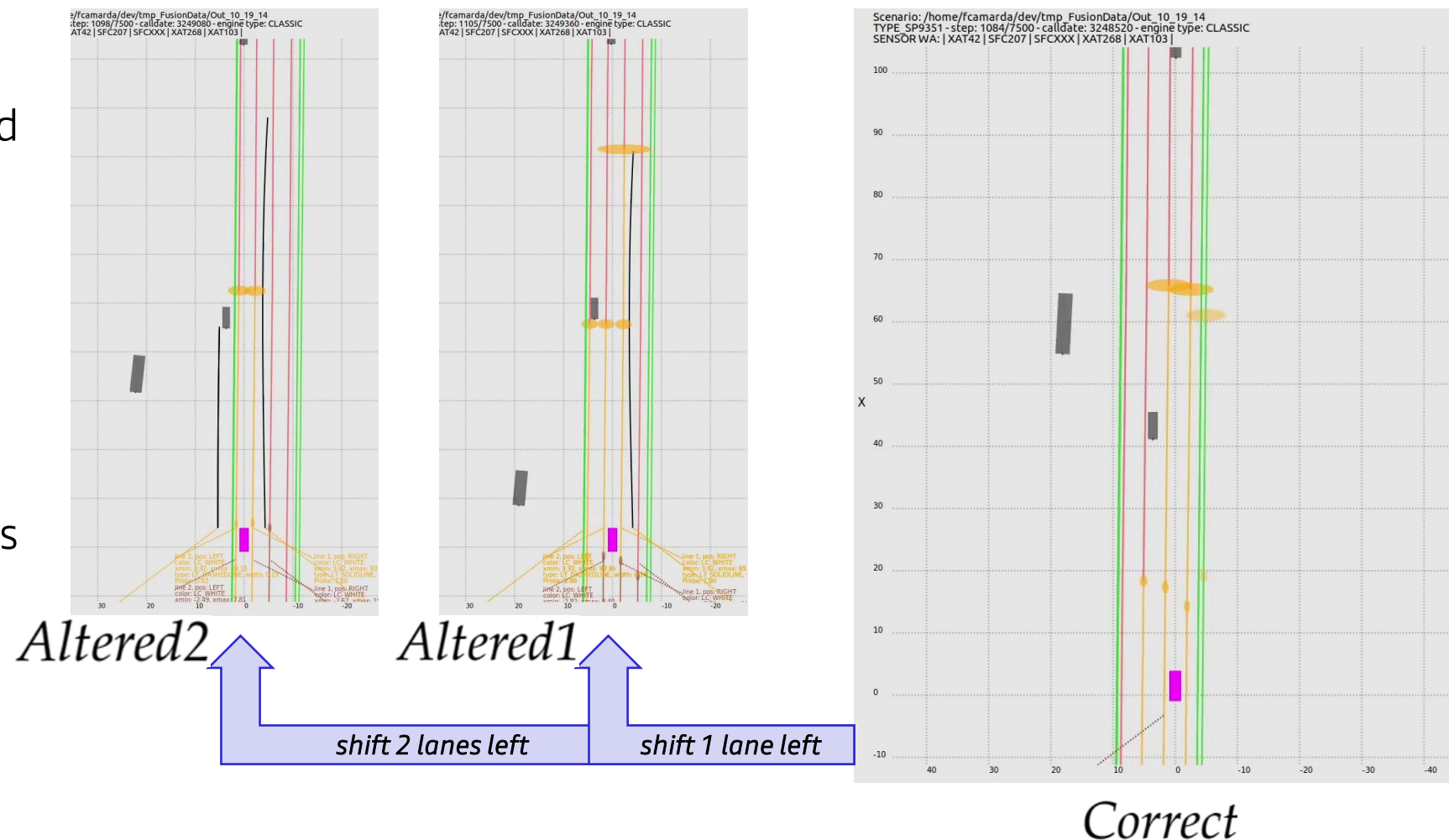
EXPERIMENTAL RESULTS : METHOD VALIDATION

- Execution in *Fusionrunner* environment : simulated localization fault generation

- In absence of better ground truth, two alterations of the recorded data are generated:

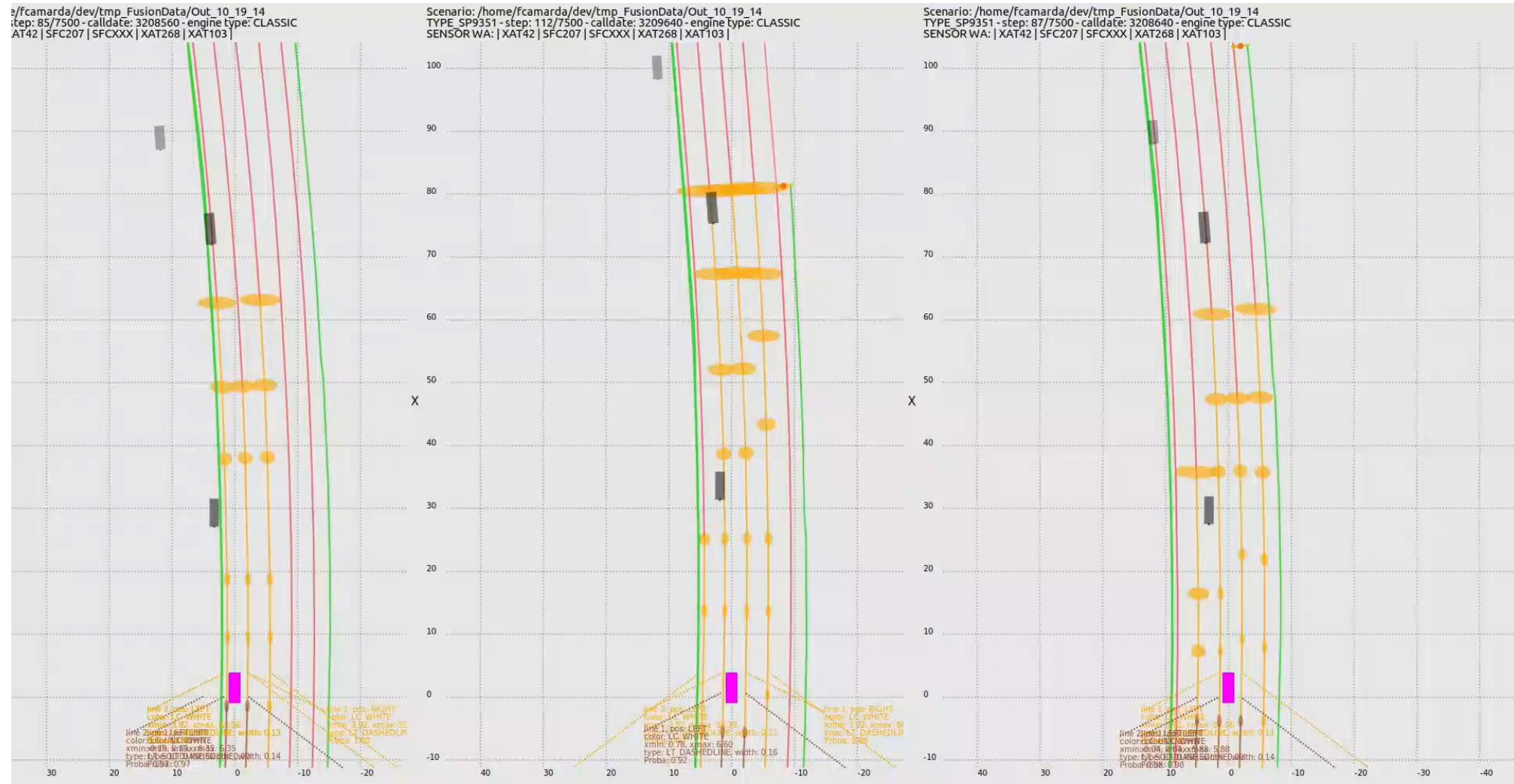
- *Correct* (authentic)
- *Altered1* (shifted 1 lane left)
- *Altered2* (shifted 2 lanes left)

- Context camera can confirm which alteration is correct



EXPERIMENTAL RESULTS : METHOD VALIDATION

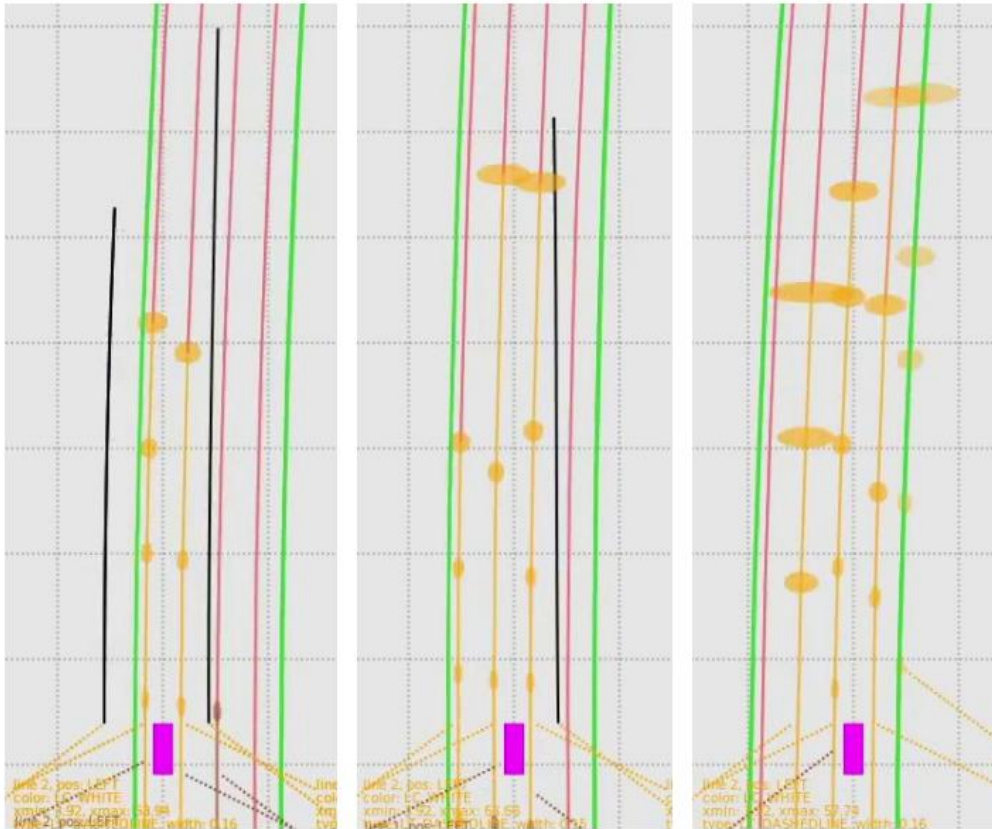
- Execution in *Fusionrunner* environment : three variations of same data record



EXPERIMENTAL RESULT : METHOD VALIDATION

- Enumerating FP and TP within a sliding window of 5 seconds, the **Precision** indicator is defined:

$$Precision(t - 5, t) = \frac{TP}{TP + FP}$$



Altered2

#FP = 2

#TP = 2

Precision = 0,5

Altered1

#FP = 1

#TP = 3

Precision = 0,75

Correct

#FP = 0

#TP = 4

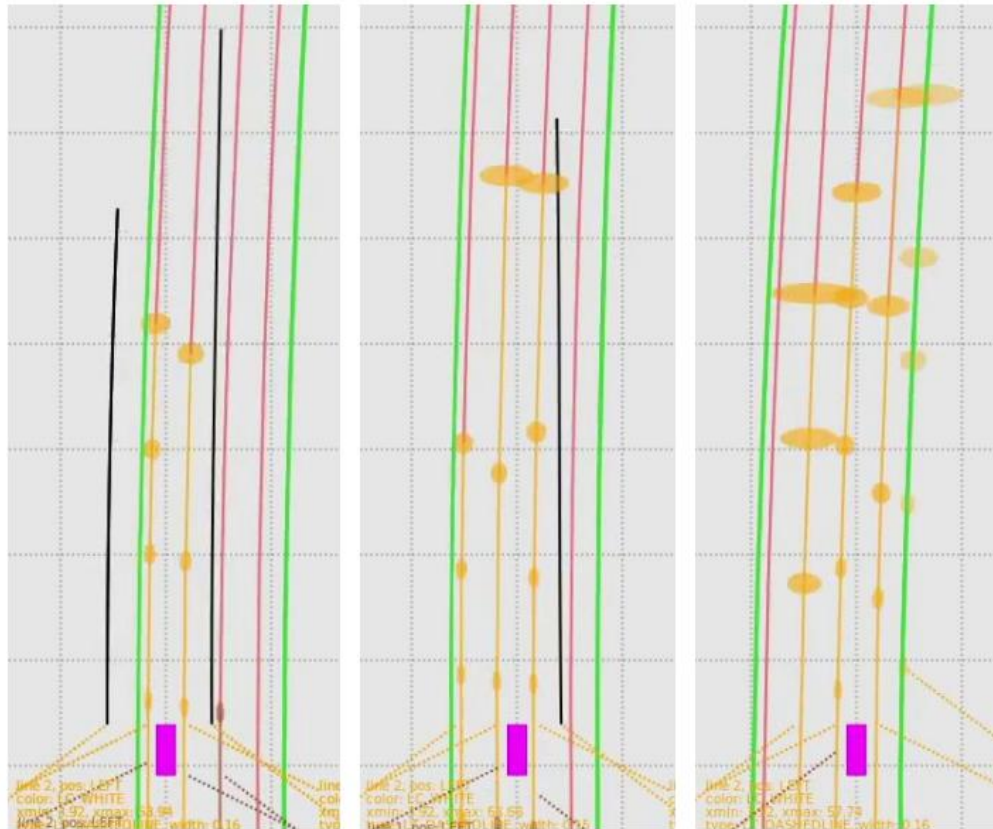
Precision = 1

EXPERIMENTAL RESULT : METHOD VALIDATION

- Enumerating FP and TP within a sliding window of 5 seconds, the **Precision** indicator is defined:

$$Precision(t - 5, t) = \frac{TP}{TP + FP}$$

Question : can the the **Precision** indicator discriminate faulty localization of ego-vehicle?



Altered2

#FP = 2

#TP = 2

Precision = 0,5

Altered1

#FP = 1

#TP = 3

Precision = 0,75

Correct

#FP = 0

#TP = 4

Precision = 1

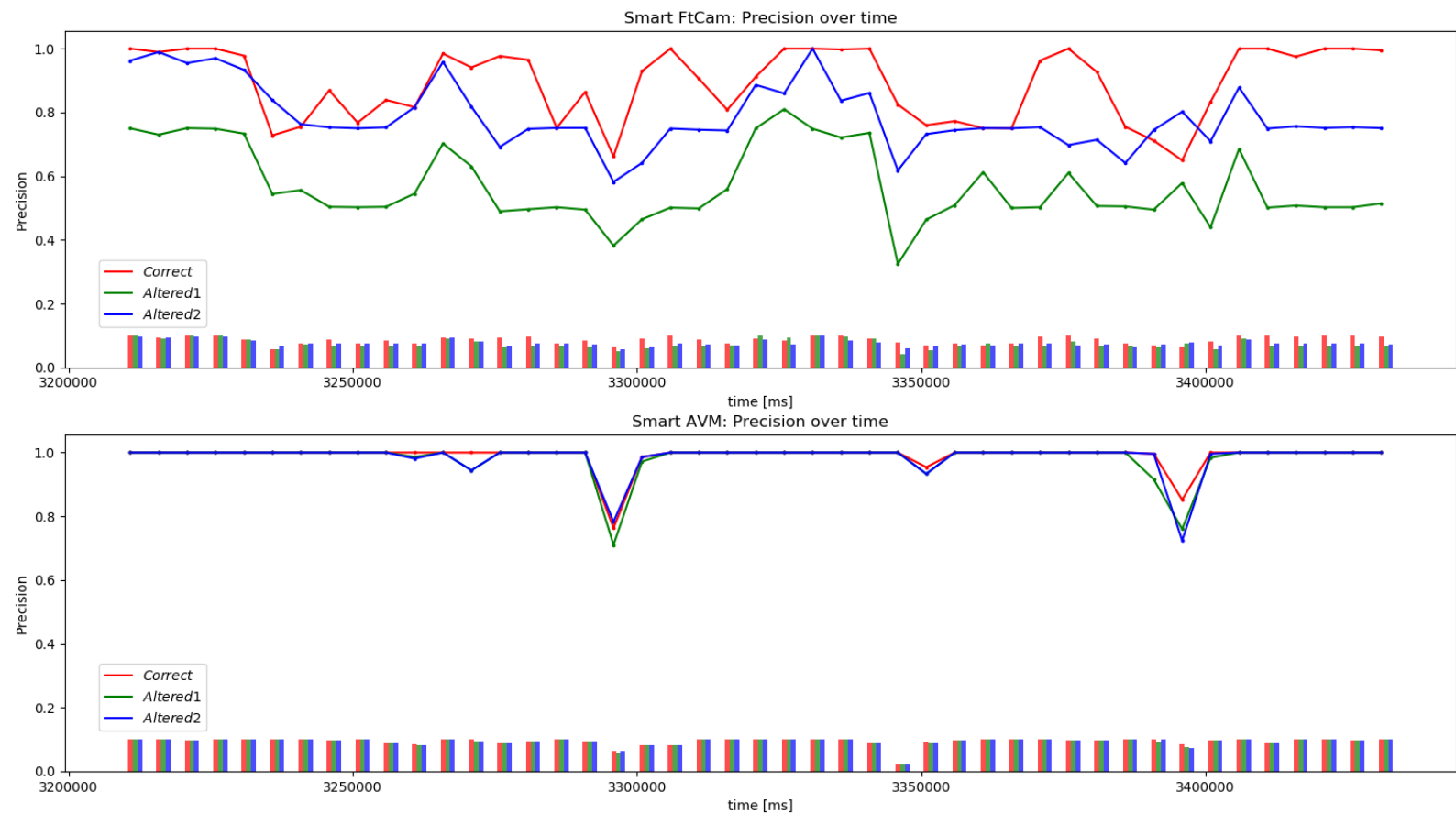
Localization
in HD-map is
incorrect

Method detects
more FPs from
sensors

Proposed association
method is validated ✓

04 MAP-AIDED MULTI-SENSOR FUSION FOR LANE BOUNDARIES ESTIMATION

EXPERIMENTAL RESULTS



— *Correct* — *Altered1* — *Altered2*

- The proposed method can **successfully detect** altered localization
 - If information in sensor delivery is enough (FrontCam > AVM)
- This detection is confirmed using Smart FrontCam and indicator *Precision(0,end)*:

	Smart FrontCam	Smart AVM
<i>Correct</i>	89.43%	99.07%
<i>Altered1</i>	57.31%	98.31%
<i>Altered2</i>	79.00%	98.60%

SECTION CONCLUSIONS

Lane boundaries probabilistic association method has been introduced and implemented

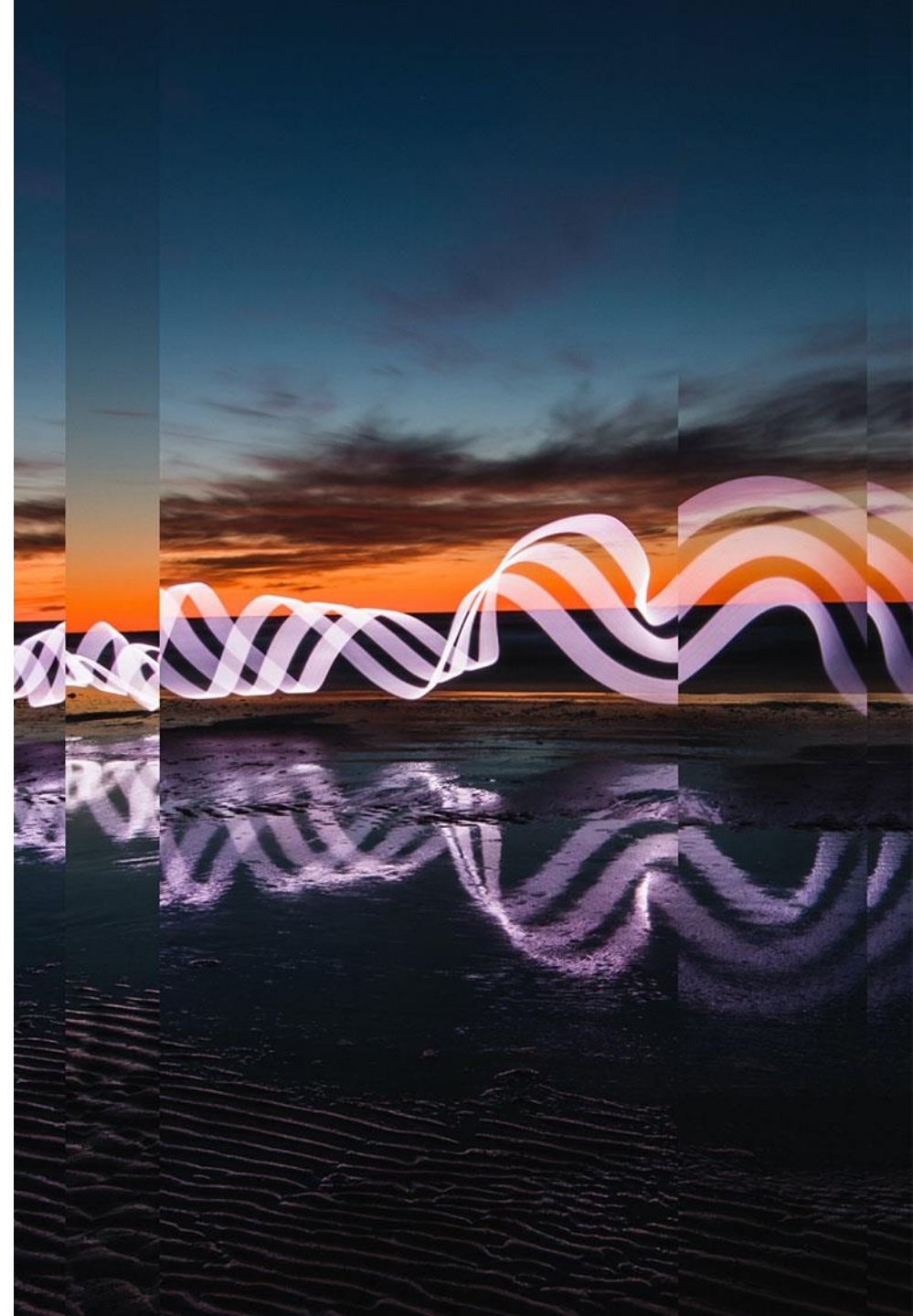
Detection of **false positives** measurements from smart sensors validated the proposed method

Application of the method for **scoring multiple hypothesis of ego-vehicle localization** reveals Smart FrontCam can better detect a localization fault rather than Smart AVM

✓ Work resulted in pending application for **Renault/UTC/CNRS patent**

05

Conclusion

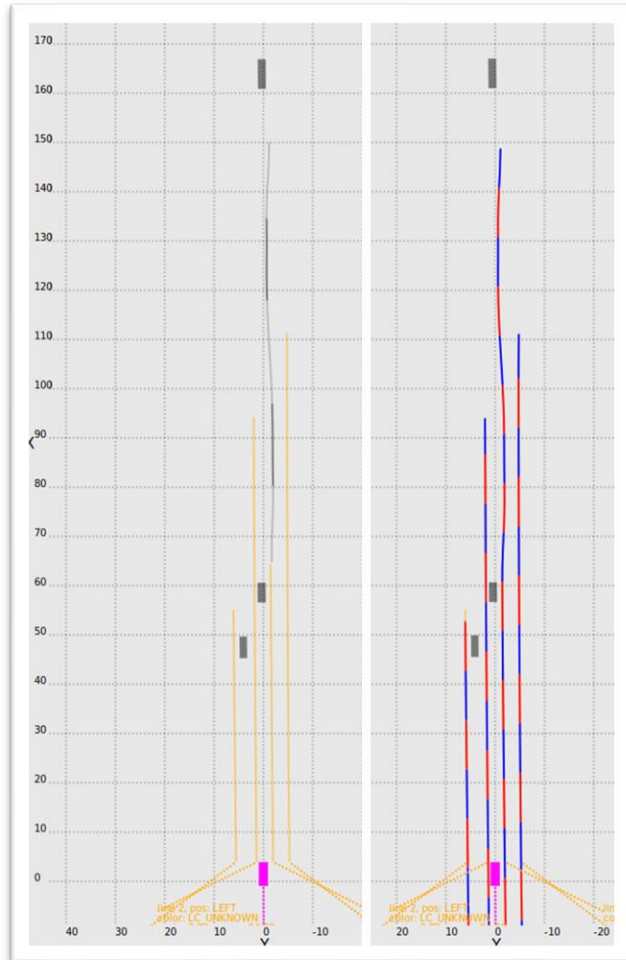


- **Feature-tracking**, method for multi-sensor fusion of lane boundaries issued of smart sensors
 - 🚗 Deployed on-vehicle in Renault L3 experimentations
- **Quantitative evaluation** w.r.t. HD-map of lane boundaries tracking methods in terms of lateral RMSE
 - 📄 Resulted in a publication at international conference IV2020
- **Lane boundaries probabilistic association** method enabling measure-to-track pairing in our tracking proposals
 - 📄 Resulted in application for Renault/CNRS patent
- **Map-tracking**, method for multi-sensor fusion of lane boundaries issued of smart sensors and map-providers (not presented)
- Usage of **Precision** metric enabling false-positives detection and multi-hypotheses localization scoring

References :

- F. Camarda, F. Davoine, V. Cherfaoui, B. Durand.** *Multisensor Tracking of Lane Boundaries based on Smart Sensor Fusion*. IEEE Intelligent Vehicles Symposium (IV 2020), Oct 2020, Las Vegas, United States.
- F. Camarda, B. Durand, F. Davoine, V. Cherfaoui.** *Procédé de détection d'une limite d'une voie de circulation*. Renault/UTC/CNRS patent. Applied for French patenting at Institut National de la Propriété Industrielle (INPI) under the identifier n°2110938, Oct 2021.

- Integrate other vehicles trails in data fusion
 - Range extension



- Release “*unvarying HD-map*” assumption
 - Lane boundaries can evolve!



The background is a deep blue gradient with numerous bright, diagonal streaks of cyan and light blue, creating a sense of motion and energy. The streaks are most prominent in the upper right and lower right areas, while the left side is a darker, more uniform blue.

Thank you

The background is a deep blue with numerous bright, diagonal streaks of cyan and light blue, creating a sense of motion and energy. The streaks vary in thickness and brightness, some appearing as sharp lines and others as softer, blurred bands.

Questions, demande, questions